CS252
Graduate Computer Architecture
Lecture 7

Cache Design (continued)

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Prof. David Culler

How to Improve Cache Performance?

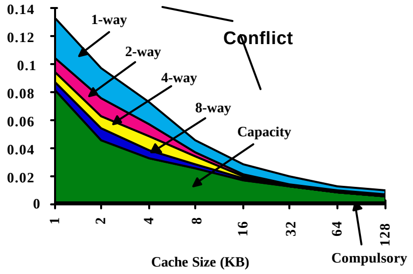
$$AMAT = HitTime + MissRate ´ MissPenalty$$

1. Reduce the miss rate,
2. Reduce the miss penalty, or
3. Reduce the time to hit in the cache.

Where to misses come from?

- Classifying Misses: 3 Cs
  - *Compulsory*—The first access to a block is not in the cache, so the block must be brought into the cache. Also called *cold start misses* or *first reference misses*. *(Misses in even an Infinite Cache)*
  - *Capacity*—If the cache cannot contain all the blocks needed during execution of a program, capacity misses will occur due to blocks being discarded and later retrieved. *(Misses in Fully Associative Size X Cache)*
  - *Conflict*—If block-placement strategy is set associative or direct mapped, conflict misses (in addition to compulsory & capacity misses) will occur because a block can be discarded and later retrieved if too many blocks map to its set. Also called *collision misses* or *interference misses*. *(Misses in N-way Associative, Size X Cache)*
- 4th "C":
  - *Coherence* - Misses caused by cache coherence.

3Cs Absolute Miss Rate (SPEC92)



Reducing Misses by Hardware Prefetching of Instructions & Data

- E.g., Instruction Prefetching
  - Alpha 21064 fetches 2 blocks on a miss
  - Extra block placed in "stream buffer"
  - On miss check stream buffer
- Works with data blocks too:
  - Jouppi [1990] 1 data stream buffer got 25% misses from 4KB cache; 4 streams got 43%
  - Palacharla & Kessler [1994] for scientific programs for 8 streams got 50% to 70% of misses from 2 64KB, 4-way set associative caches
- Prefetching relies on having extra memory bandwidth that can be used without penalty

Reducing Misses by Software Prefetching Data

- Data Prefetch
  - Load data into register (HP PA-RISC loads)
  - Cache Prefetch: load into cache (MIPS IV, PowerPC, SPARC v. 9)
  - Special prefetching instructions cannot cause faults; a form of speculative execution
- Prefetching comes in two flavors:
  - Binding prefetch: Requests load directly into register.
    - » Must be correct address and register!
  - Non-Binding prefetch: Load into cache.
    - » Can be incorrect. Faults?
- Issuing Prefetch Instructions takes time
  - Is cost of prefetch issues < savings in reduced misses?
  - Higher superscalar reduces difficulty of issue bandwidth

Reducing Misses by Compiler Optimizations

- McFarling [1989] reduced caches misses by 75% on 8KB direct mapped cache, 4 byte blocks in software
- Instructions
  - Reorder procedures in memory so as to reduce conflict misses
  - Profiling to look at conflicts(using tools they developed)
- Data
  - *Merging Arrays*: improve spatial locality by single array of compound elements vs. 2 arrays
  - *Loop Interchange*: change nesting of loops to access data in order stored in memory
  - *Loop Fusion*: Combine 2 independent loops that have same looping and some variables overlap
  - *Blocking*: Improve temporal locality by accessing "blocks" of data repeatedly vs. going down whole columns or rows

Merging Arrays Example

```
/* Before: 2 sequential arrays */
int val[SIZE];
int key[SIZE];

/* After: 1 array of stuctures */
struct merge {
  int val;
  int key;
};
struct merge merged_array[SIZE];
```

Reducing conflicts between val & key; improve spatial locality

Loop Interchange Example

```
/* Before */
for (k = 0; k < 100; k = k+1)
  for (j = 0; j < 100; j = j+1)
      for (i = 0; i < 5000; i = i+1)
           x[i][j] = 2 * x[i][j];
/* After */
for (k = 0; k < 100; k = k+1)
  for (i = 0; i < 5000; i = i+1)
      for (j = 0; j < 100; j = j+1)
           x[i][j] = 2 * x[i][j];
```

Sequential accesses instead of striding through memory every 100 words; improved spatial locality

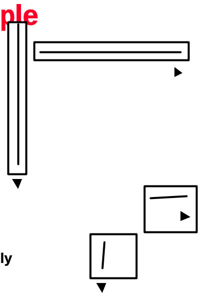
Loop Fusion Example

```
/* Before */
for (i = 0; i < N; i = i+1)
  for (j = 0; j < N; j = j+1)
      a[i][j] = 1/b[i][j] * c[i][j];
for (i = 0; i < N; i = i+1)
  for (j = 0; j < N; j = j+1)
      d[i][j] = a[i][j] + c[i][j];
/* After */
for (i = 0; i < N; i = i+1)
  for (j = 0; j < N; j = j+1)
  {   a[i][j] = 1/b[i][j] * c[i][j];
      d[i][j] = a[i][j] + c[i][j];}
```

2 misses per access to a & c vs. one miss per access; improve spatial locality

Blocking Example

```
/* Before */
for (i = 0; i < N; i = i+1)
  for (j = 0; j < N; j = j+1)
     {r = 0;
      for (k = 0; k < N; k = k+1){
        r = r + y[i][k]*z[k][j];};
      x[i][j] = r;
     };
```

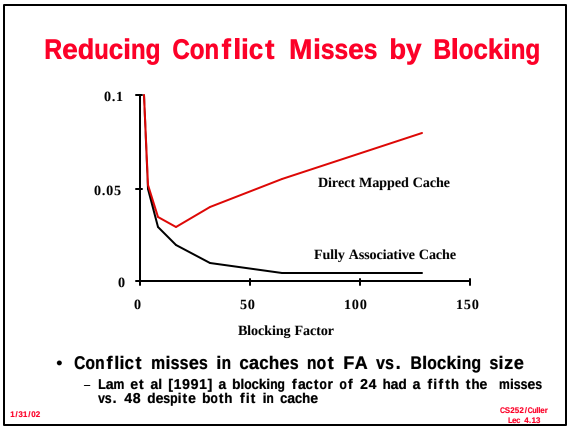


- Two Inner Loops:
  - Read all NxN elements of z[]
  - Read N elements of 1 row of y[] repeatedly
  - Write N elements of 1 row of x[]
- Capacity Misses a function of N & Cache Size:
  - $2N^3 + N^2$ => (assuming no conflict; otherwise …)
- Idea: compute on BxB submatrix that fits

Blocking Example

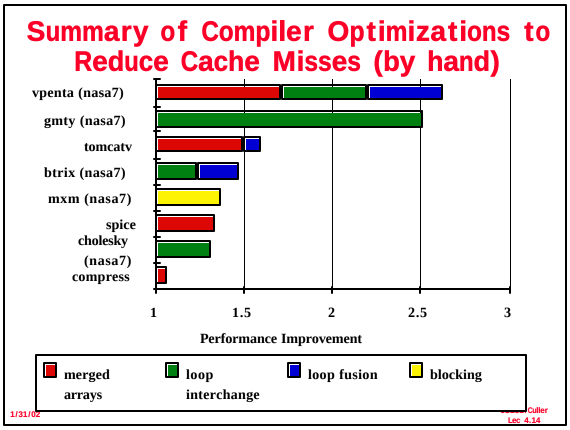
```
/* After */
for (jj = 0; jj < N; jj = jj+B)
for (kk = 0; kk < N; kk = kk+B)
for (i = 0; i < N; i = i+1)
   for (j = jj; j < min(jj+B-1,N); j = j+1)
     {r = 0;
      for (k = kk; k < min(kk+B-1,N); k = k+1) {
        r = r + y[i][k]*z[k][j];};
      x[i][j] = x[i][j] + r;
     };
```

- B called *Blocking Factor*
- Capacity Misses from $2N^3 + N^2$ to $N^3/B+2N^2$
- Conflict Misses Too?

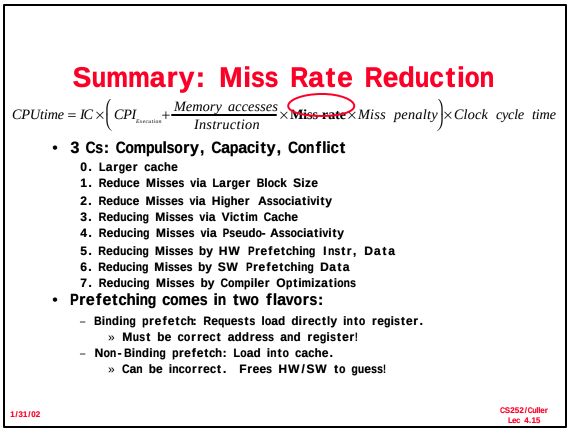


Reducing Conflict Misses by Blocking

- Conflict misses in caches not FA vs. Blocking size
  - Lam et al [1991] a blocking factor of 24 had a fifth the misses vs. 48 despite both fit in cache



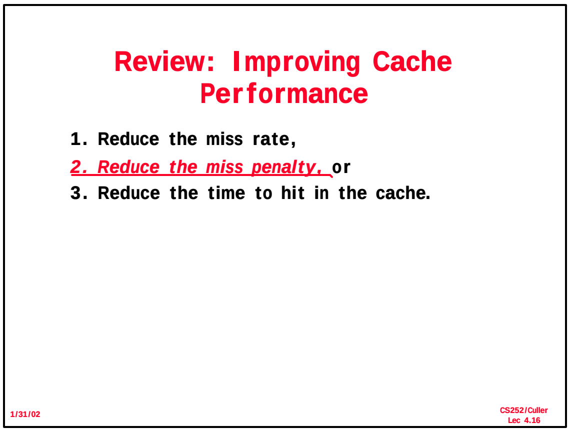
Summary of Compiler Optimizations to Reduce Cache Misses (by hand)



Summary: Miss Rate Reduction

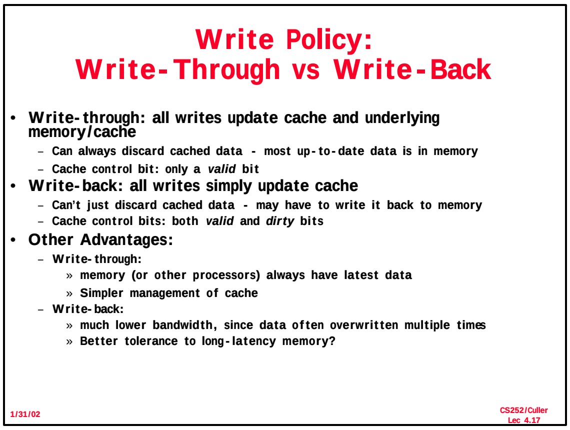
$$CPUtime = IC \times \left(CPI_{Execution} + \frac{Memory\ \ accesses}{Instruction} \times \cancel{\text{Miss rate}} \times Miss\ \ penalty \right) \times Clock\ \ cycle\ \ time$$

- 3 Cs: Compulsory, Capacity, Conflict
  0. Larger cache
  1. Reduce Misses via Larger Block Size
  2. Reduce Misses via Higher Associativity
  3. Reducing Misses via Victim Cache
  4. Reducing Misses via Pseudo-Associativity
  5. Reducing Misses by HW Prefetching Instr, Data
  6. Reducing Misses by SW Prefetching Data
  7. Reducing Misses by Compiler Optimizations
- Prefetching comes in two flavors:
  - Binding prefetch: Requests load directly into register.
    - » Must be correct address and register!
  - Non-Binding prefetch: Load into cache.
    - » Can be incorrect. Frees HW/SW to guess!



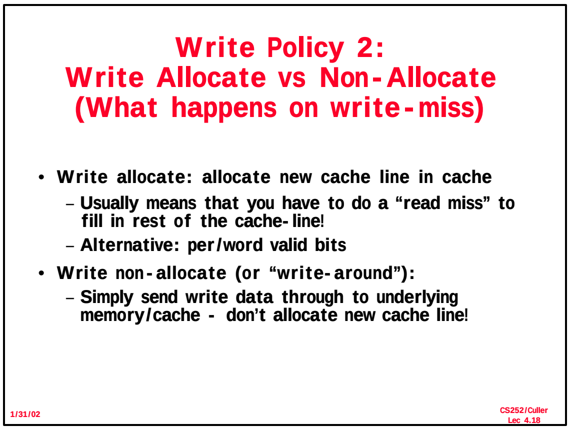
Review: Improving Cache Performance

1. Reduce the miss rate,
2. *Reduce the miss penalty,* or
3. Reduce the time to hit in the cache.



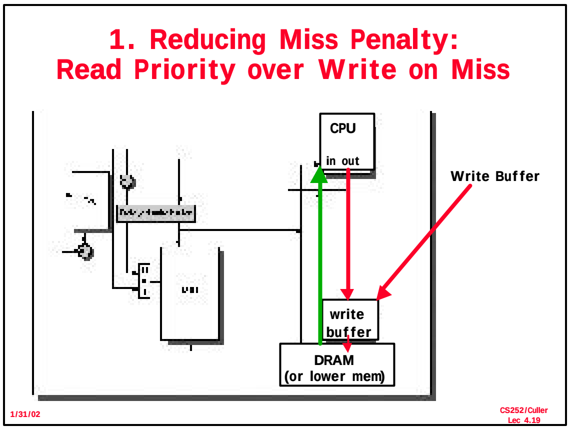
Write Policy: Write-Through vs Write-Back

- Write-through: all writes update cache and underlying memory/cache
  - Can always discard cached data - most up-to-date data is in memory
  - Cache control bit: only a *valid* bit
- Write-back: all writes simply update cache
  - Can't just discard cached data - may have to write it back to memory
  - Cache control bits: both *valid* and *dirty* bits
- Other Advantages:
  - Write-through:
    - » memory (or other processors) always have latest data
    - » Simpler management of cache
  - Write-back:
    - » much lower bandwidth, since data often overwritten multiple times
    - » Better tolerance to long-latency memory?

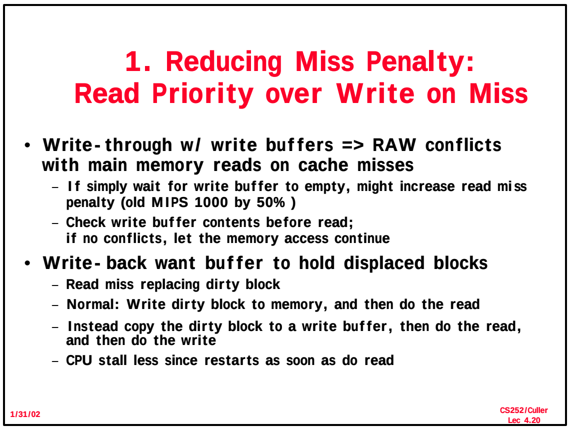


Write Policy 2: Write Allocate vs Non-Allocate (What happens on write-miss)

- Write allocate: allocate new cache line in cache
  - Usually means that you have to do a "read miss" to fill in rest of the cache-line!
  - Alternative: per/word valid bits
- Write non-allocate (or "write-around"):
  - Simply send write data through to underlying memory/cache - don't allocate new cache line!

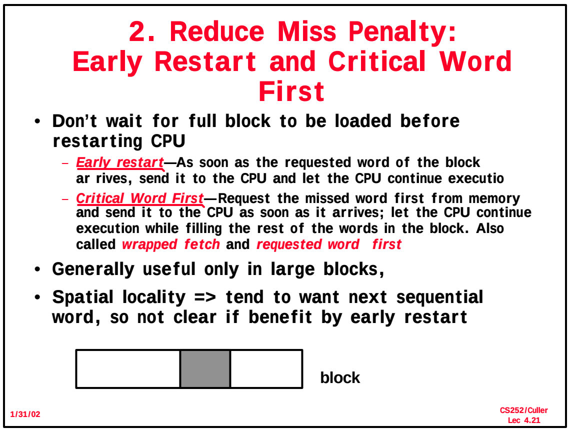


1. Reducing Miss Penalty: Read Priority over Write on Miss



1. Reducing Miss Penalty: Read Priority over Write on Miss

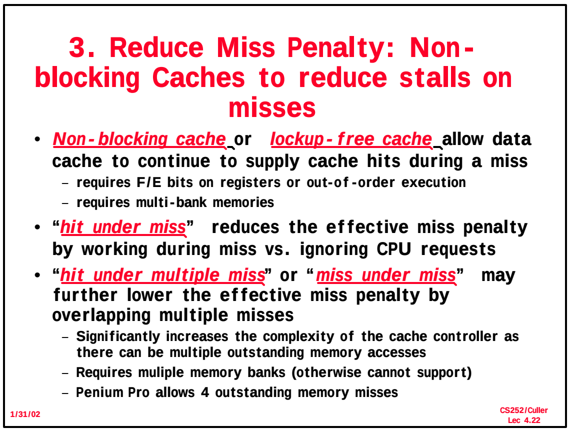
- Write-through w/ write buffers => RAW conflicts with main memory reads on cache misses
  - If simply wait for write buffer to empty, might increase read miss penalty (old MIPS 1000 by 50%)
  - Check write buffer contents before read; if no conflicts, let the memory access continue
- Write-back want buffer to hold displaced blocks
  - Read miss replacing dirty block
  - Normal: Write dirty block to memory, and then do the read
  - Instead copy the dirty block to a write buffer, then do the read, and then do the write
  - CPU stall less since restarts as soon as do read



2. Reduce Miss Penalty: Early Restart and Critical Word First

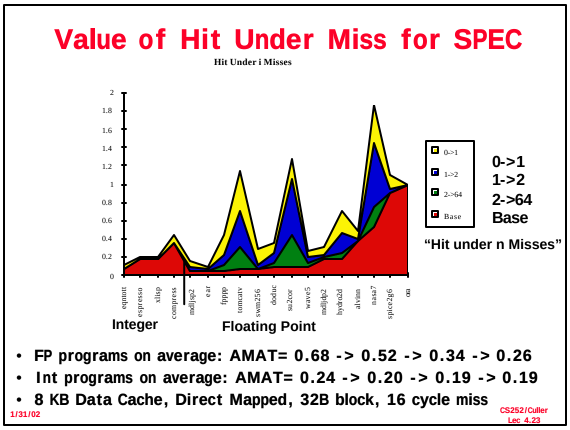
- Don't wait for full block to be loaded before restarting CPU
  - *Early restart*—As soon as the requested word of the block ar rives, send it to the CPU and let the CPU continue executio
  - *Critical Word First*—Request the missed word first from memory and send it to the CPU as soon as it arrives; let the CPU continue execution while filling the rest of the words in the block. Also called *wrapped fetch* and *requested word first*
- Generally useful only in large blocks,
- Spatial locality => tend to want next sequential word, so not clear if benefit by early restart

block



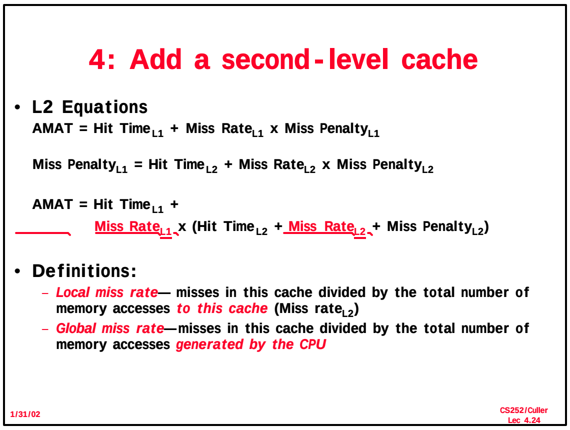
3. Reduce Miss Penalty: Non-blocking Caches to reduce stalls on misses

- *Non-blocking cache* or *lockup-free cache* allow data cache to continue to supply cache hits during a miss
  - requires F/E bits on registers or out-of-order execution
  - requires multi-bank memories
- "*hit under miss*" reduces the effective miss penalty by working during miss vs. ignoring CPU requests
- "*hit under multiple miss*" or "*miss under miss*" may further lower the effective miss penalty by overlapping multiple misses
  - Significantly increases the complexity of the cache controller as there can be multiple outstanding memory accesses
  - Requires muliple memory banks (otherwise cannot support)
  - Penium Pro allows 4 outstanding memory misses



Value of Hit Under Miss for SPEC

- FP programs on average: AMAT= 0.68 -> 0.52 -> 0.34 -> 0.26
- Int programs on average: AMAT= 0.24 -> 0.20 -> 0.19 -> 0.19
- 8 KB Data Cache, Direct Mapped, 32B block, 16 cycle miss



4: Add a second-level cache

- L2 Equations

  AMAT = Hit Time_{L1} + Miss Rate_{L1} x Miss Penalty_{L1}

  Miss Penalty_{L1} = Hit Time_{L2} + Miss Rate_{L2} x Miss Penalty_{L2}

  AMAT = Hit Time_{L1} +

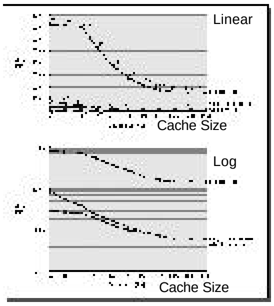
  Miss Rate_{L1} x (Hit Time_{L2} + Miss Rate_{L2} + Miss Penalty_{L2})
- Definitions:
  - *Local miss rate*— misses in this cache divided by the total number of memory accesses *to this cache* (Miss rate_{L2})
  - *Global miss rate*—misses in this cache divided by the total number of memory accesses *generated by the CPU*

Partner Discussion

What's different in L2 vs L1 Caches?

Comparing Local and Global Miss Rates

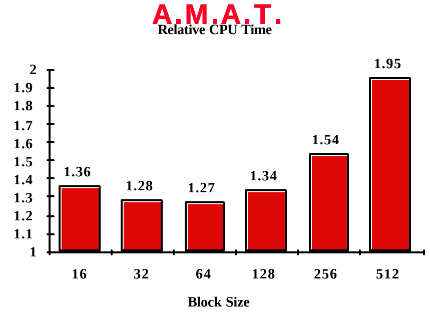
- 32 KByte 1st level cache; Increasing 2nd level cache
- Global miss rate close to single level cache rate provided L2 >> L1
- Don't use local miss rate
- L2 not tied to CPU clock cycle!
- Cost & A.M.A.T.
- Generally Fast Hit Times and fewer misses
- Since hits are few, target miss reduction



Reducing Misses: Which apply to L2 Cache?

- Reducing Miss Rate
  1. Reduce Misses via Larger Block Size
  2. Reduce Conflict Misses via Higher Associativity
  3. Reducing Conflict Misses via Victim Cache
  4. Reducing Conflict Misses via Pseudo-Associativity
  5. Reducing Misses by HW Prefetching Instr, Data
  6. Reducing Misses by SW Prefetching Data
  7. Reducing Capacity/Conf. Misses by Compiler Optimizations

L2 cache block size & A.M.A.T.



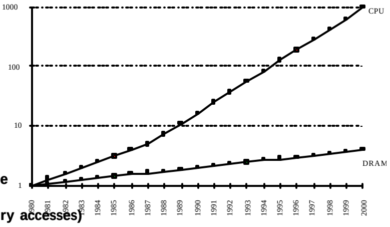
- 32KB L1, 8 byte path to memory

Reducing Miss Penalty Summary

$$CPUtime = IC \times \left(CPI_{Execution} + \frac{Memory\ \ accesses}{Instruction} \times \textbf{Miss rate} \times Miss\ \ penalty \right) \times Clock\ \ cycle\ \ time$$

- Four techniques
  - Read priority over write on miss
  - Early Restart and Critical Word First on miss
  - Non-blocking Caches (Hit under Miss, Miss under Miss)
  - Second Level Cache
- Can be applied recursively to Multilevel Caches
  - Danger is that time to DRAM will grow with multiple levels in between
  - First attempts at L2 caches can make things worse, since increased worst case is worse

What is the Impact of What You've Learned About Caches?

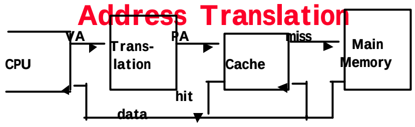


- 1960-1985: Speed = ƒ(no. operations)
- 1990
  - Pipelined Execution & Fast Clock Rate
  - Out-of-Order execution
  - Superscalar Instruction Issue
- 1998: Speed = ƒ(non-cached memory accesses)
- Superscalar, Out-of-Order machines hide L1 data cache miss (-5 clocks) but not L2 cache miss (-50 clocks)?

1. Fast Hit times via Small and Simple Caches

- Why Alpha 21164 has 8KB Instruction and 8KB data cache + 96KB second level cache?
  - Small data cache and clock rate
- Direct Mapped, on chip

Address Translation



- Page table is a large data structure in memory
- Two memory accesses for every load, store, or instruction fetch!!!
- Virtually addressed cache?
  - synonym problem
- Cache the address translations?

TLBs

A way to speed up translation is to use a special cache of recently used page table entries -- this has many names, but the most frequently used is *Translation Lookaside Buffer or TLB*

Virtual Address	Physical Address	Dirty	Ref	Valid	Access

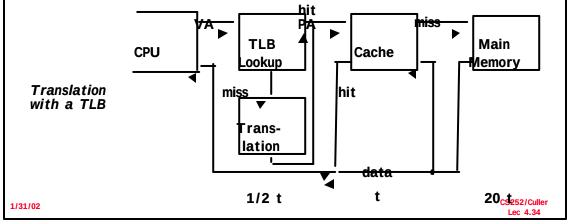
Really just a cache on the page table mappings

TLB access time comparable to cache access time (much less than main memory access time)

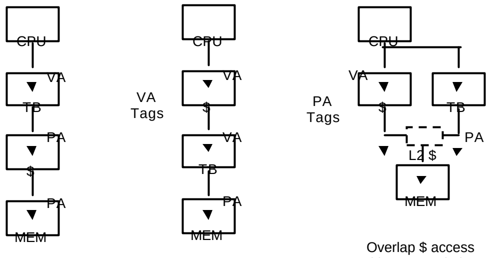
Translation Look-Aside Buffers

Just like any other cache, the TLB can be organized as fully associative, set associative, or direct mapped

TLBs are usually small, typically not more than 128 - 256 entries even on high end machines. This permits fully associative lookup on these machines. Most mid-range machines use small n-way set associative organizations.



2. Fast hits by Avoiding Address Translation



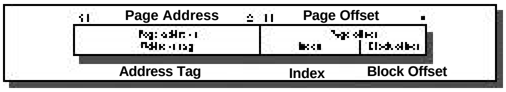
Conventional Organization

Virtually Addressed Cache
Translate only on miss
Synonym Problem

Overlap $ access with VA translation: requires $ index to remain invariant across translation

2. Fast Cache Hits by Avoiding Translation: Index with Physical Portion of Address

- If index is physical part of address, can start tag access in parallel with translation so that can compare to physical tag



- Limits cache to page size: what if want bigger caches and uses same trick?
  - Higher associativity moves barrier to right
  - Page coloring

2. Fast hits by Avoiding Address Translation

- Send virtual address to cache? Called *Virtually Addressed Cache* or just *Virtual Cache* vs. *Physical Cache*
  - Every time process is switched logically must flush the cache; otherwise get false hits
    - » Cost is time to flush + "compulsory" misses from empty cache
    - » Add *process identifier tag* that identifies process as well as address within process: can't get a hit if wrong process
- Dealing with *aliases* (sometimes called *synonyms*); Two different virtual addresses map to same physical address
  - solve by fiat: noaliasing! What are the implications?
  - HW antialiasing: guarantees every cache block has unique address
    - » verify on miss (rather than on every hit)
    - » cache set size <= page size ?
    - » what if it gets larger?
  - How can SW simplify the problem? (called *page coloring)*
  - I/O must interact with cache, so need virtual address

3: Fast Hits by pipelining Cache Case Study: MIPS R4000

- 8 Stage Pipeline:
  - IF–first half of fetching of instruction; PC selection happens here as well as initiation of instruction cache access.
  - IS–second half of access to instruction cache.
  - RF–instruction decode and register fetch, hazard checking and also instruction cache hit detection.
  - EX–execution, which includes effective address calculation, ALU operation, and branch target computation and condition evaluation.
  - DF–data fetch, first half of access to data cache.
  - DS–second half of access to data cache.
  - TC–tag check, determine whether the data cache access hit.
  - WB–write back for loads and register-register operations.
- What is impact on Load delay?
  - Need 2 instructions between a load and its use!

Case Study: MIPS R4000

TWO Cycle Load Latency

IF	IS	RF	EX	DF	DS	TC	WB
	IF	IS	RF	EX	DF	DS	TC
		IF	IS	RF	EX	DF	DS
			IF	IS	RF	EX	DF
				IF	IS	RF	EX
					IF	IS	RF
						IF	IS
							IF

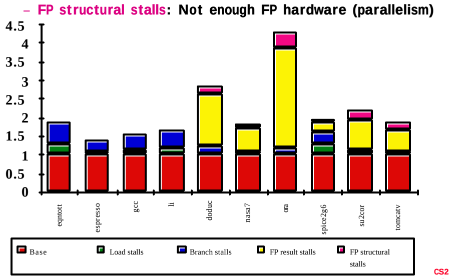
THREE Cycle Branch Latency
(conditions evaluated during EX phase)

IF	IS	RF	EX	DF	DS	TC	WB
	IF	IS	RF	EX	DF	DS	TC
		IF	IS	RF	EX	DF	DS
			IF	IS	RF	EX	DF
				IF	IS	RF	EX
					IF	IS	RF
						IF	IS
							IF

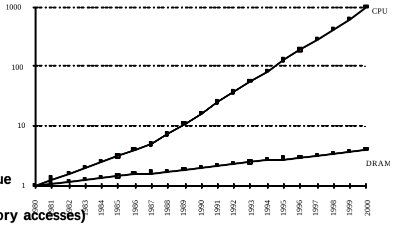
Delay slot plus two stalls
Branch likely cancels delay slot if not taken

R4000 Performance

- Not ideal CPI of 1:
  - Load stalls (1 or 2 clock cycles)
  - Branch stalls (2 cycles + unfilled slots)
  - FP result stalls: RAW data hazard (latency)
  - FP structural stalls: Not enough FP hardware (parallelism)



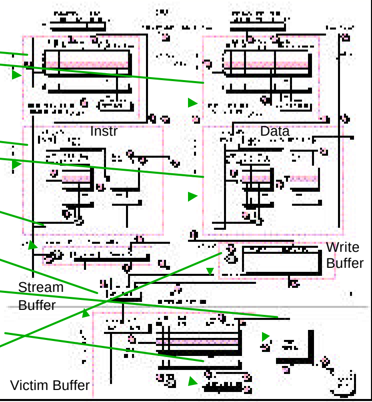
What is the Impact of What You've Learned About Caches?

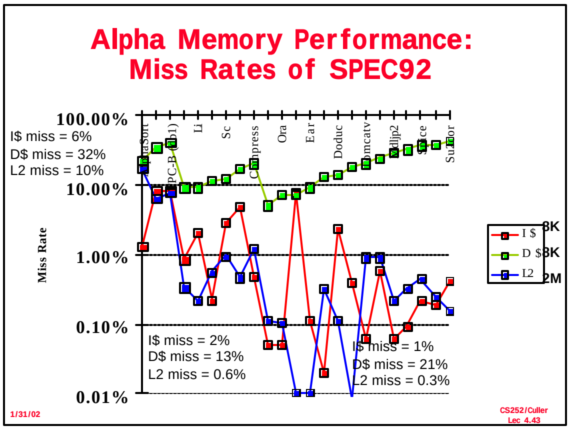


- 1960-1985: Speed = *f*(no. operations)
- 1990
  - Pipelined Execution & Fast Clock Rate
  - Out-of-Order execution
  - Superscalar Instruction Issue
- 1998: Speed = *f*(non-cached memory accesses)
- What does this mean for
  - Compilers?,Operating Systems?, Algorithms? Data Structures?

Alpha 21064

- Separate Instr & Data TLB & Caches
- TLBs fully associative
- TLB updates in SW ("Priv Arch Libr")
- Caches 8KB direct mapped, write thru
- Critical 8 bytes first
- Prefetch instr. stream buffer
- 2 MB L2 cache, direct mapped, WB (off-chip)
- 256 bit path to main memory, 4 x 64-bit modules
- Victim Buffer: to give read priority over write
- 4 entry write buffer between D$ & L2$





Alpha Memory Performance: Miss Rates of SPEC92

I$ miss = 6%
D$ miss = 32%
L2 miss = 10%

I$ miss = 2%
D$ miss = 13%
L2 miss = 0.6%

I$ miss = 1%
D$ miss = 21%
L2 miss = 0.3%

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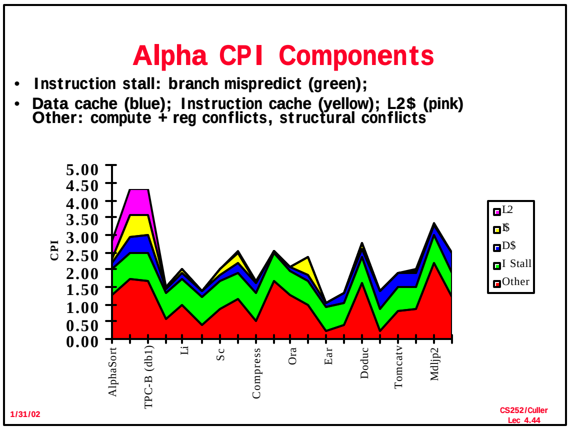
CS252/Culler
Lec 4.43



Alpha CPI Components

- Instruction stall: branch mispredict (green);
- Data cache (blue); Instruction cache (yellow); L2$ (pink)
  Other: compute + reg conflicts, structural conflicts

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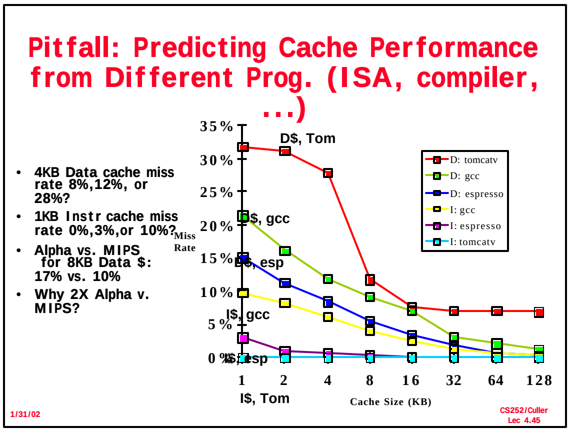
CS252/Culler
Lec 4.44

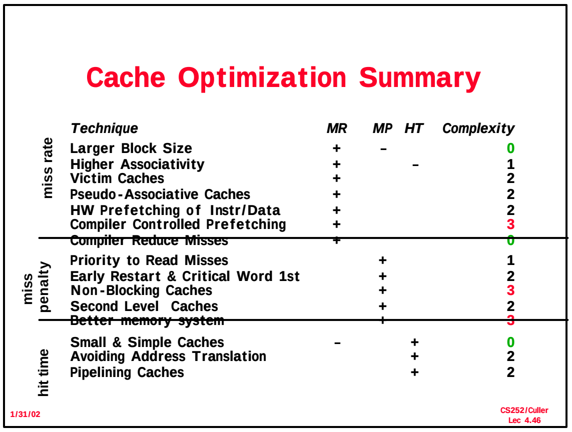


Pitfall: Predicting Cache Performance from Different Prog. (ISA, compiler, ...)

- 4KB Data cache miss rate 8%,12%, or 28%?
- 1KB Instr cache miss rate 0%,3%,or 10%?
- Alpha vs. MIPS for 8KB Data $: 17% vs. 10%
- Why 2X Alpha v. MIPS?

1/31/02

CS252/Culler
Lec 4.45



Cache Optimization Summary

	Technique	*MR*	*MP*	*HT*	*Complexity*
miss rate	Larger Block Size	+	–		0
	Higher Associativity	+		–	1
	Victim Caches	+			2
	Pseudo-Associative Caches	+			2
	HW Prefetching of Instr/Data	+			2
	Compiler Controlled Prefetching	+			3
	Compiler Reduce Misses	+			0
miss penalty	Priority to Read Misses		+		1
	Early Restart & Critical Word 1st		+		2
	Non-Blocking Caches		+		3
	Second Level Caches		+		2
	Better memory system		+		3
hit time	Small & Simple Caches	–		+	0
	Avoiding Address Translation			+	2
	Pipelining Caches			+	2

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