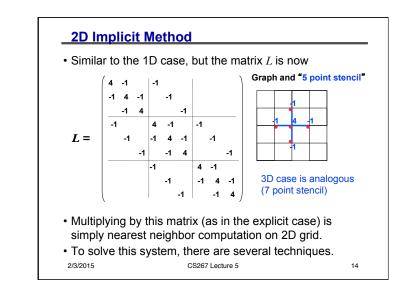


Algorithm	Serial	PRAM	Memory	#Proce
Dense LU	N <sup>3</sup>	N	N <sup>2</sup>	N <sup>2</sup>
<ul> <li>Band LU</li> </ul>	N <sup>2</sup> (N <sup>7/3</sup> )	Ν	N <sup>3/2</sup> (N <sup>5/3</sup> )	N(N <sup>4/3</sup> )
<ul> <li>Jacobi</li> </ul>	N <sup>2</sup> (N <sup>5/3</sup> )	N (N <sup>2/3</sup> )	N	Ν
<ul> <li>Explicit Inv.</li> </ul>	N <sup>2</sup>	log N	N <sup>2</sup>	N <sup>2</sup>
· Conj.Gradients	N <sup>3/2</sup> (N <sup>4/3</sup> )	N <sup>1/2 (1/3)</sup> *log N	N	Ν
· Red/Black SOF	RN <sup>3/2</sup> (N <sup>4/3</sup> )	N <sup>1/2</sup> (N <sup>4/3</sup> )	N	Ν
<ul> <li>Sparse LU</li> </ul>	N <sup>3/2</sup> (N <sup>2</sup> )	N <sup>1/2</sup> (N <sup>2/3</sup> )	N*log N (N <sup>4/3</sup> )	N(N <sup>4/3</sup> )
• FFT	N*log N	log N	N	Ν
<ul> <li>Multigrid</li> </ul>	Ν	log <sup>2</sup> N	N	Ν
Lower bound	Ν	log N	Ν	
PRAM is an idea References: Jan Decision tree to I	lized parallel m nes Demmel, A nelp choose alg		near Algebra, SIAM	1, 1997.
www.netli	b.org/linalg/htm	nl_templates/Templates	tes.html	
		CS267 Lecture 5		15



<ul> <li>Sorted in two orders (r</li> </ul>	oughly):	
<ul> <li>from slowest to fastes</li> </ul>	on sequential machines.	
<ul> <li>from most general (wo</li> </ul>	rks on any matrix) to most specialized (works	on matrices "like" T).
<ul> <li>Dense LU: Gaussian e</li> </ul>	limination; works on any N-by-N matrix.	
• Band LU: Exploits the diagonal.	fact that T is nonzero only on sqrt(N) dia	gonals nearest mair
<ul> <li>Jacobi: Essentially doe algorithm.</li> </ul>	es matrix-vector multiply by T in inner loc	p of iterative
	ne we want to solve many systems with inv(T) "for free", and just multiply by it (I	
	ses matrix-vector multiplication, like Jacos of T that Jacobi does not.	obi, but exploits
	essive over-relaxation): Variation of Jaco properties of T. Used in multigrid schen	
Sparse LU: Gaussian	elimination exploiting particular zero stru	cture of T.
FFT (Fast Fourier Tran	nsform): Works only on matrices very like	e T.
Multigrid: Also works c	n matrices like T, that come from elliptic	PDEs.
Lower Bound: Serial (t	ime to print answer); parallel (time to cor	nbine N inputs).
Details in class notes a	and www.cs.berkeley.edu/~demmel/ma2	21.
2/3/2015	CS267 Lecture 5	16

Mflop/s Versus Run Time in Practice									
	<ul> <li>Problem: Iterative solver for a convection-diffusion problem; run on a 1024-CPU NCUBE-2.</li> <li>Reference: Shadid and Tuminaro, SIAM Parallel Processing Conference, March 1991.</li> </ul>								
	Solver	Flops	CPU Time(s) I						
	Jacobi	3.82x10 <sup>12</sup>	2124	1800					
	Gauss-Seidel	1.21x10 <sup>12</sup>	885	1365					
	Multigrid	2.13x10 <sup>9</sup>	7	318					
Which solver would you select?									
	2/3/2015 CS267 Lecture 5								

