


## Learnability: [Gold 67]

- Criterion: identification in the limit
- A presentation of $L$ is an infinite sequence of $x$ 's from $L$ in which each $x$ occurs at least once
- A learner H identifies L in the limit if for any presentation of L , from some point n onward, H always outputs L
- A class $\mathscr{L}$ is identifiable in the limit if there is some single H which correctly identifies in the limit any L in $\mathscr{L}$
- Example: $L=\{\{a\},\{a, b\}\}$ is learnable in the limit
- Theorem [Gold 67]: Any $\mathscr{L}$ which contains all finite languages and at least one infinite language (i.e. is superfinite) is unlearnable in this sense


## Learnability: [Gold 67]

## - Proof sketch

- Assume $\mathscr{L}$ is superfinite
- There exists a chain $L_{1} \subset L_{2} \subset \ldots L_{\infty}$
- Take any learner H assumed to identify $\mathscr{L}$
- Construct the following misleading sequence
- Present strings from $L_{1}$ until it outputs $L_{1}$
- Present strings from $L_{2}$ until it outputs $L_{2}$
- ..
- This is a presentation of $\mathrm{L}_{\infty}$, but H won't identify $\mathrm{L}_{\infty}$


## Learnability: [Horning 69]

- Proof sketch
- Assume $s$ is a recursively enumerable set of recursive languages (e.g. the set of PCFGs)
- Assume an ordering on all strings $x_{1}<x_{2}<$.
- Define: two sequences $A$ and $B$ agree through $n$ if for all $x<x_{n}, x$ in $A \Leftrightarrow x$ in B
- Define the error set $E(L, n, m)$ :
- All sequences such that the first $m$ elements do not agree with $L$ through $n$
- These are the sequences which contain early strings outside of $L$ (can't happen)
or fail to contain all the early strings in $L$ (happens less as $m$ increases) or fail to contain all the early strings in $L$ (happens less as $m$ increases)
- Claim: $P(E(L, n, m))$ goes to 0 as $m$ goes to $\infty$
- Let $d_{L}(n)$ be the smallest $m$ such that $P(E)<2^{-n}$
- Let $d(n)$ be the largest $d_{L}(n)$ in first $n$ languages
- Learner: after $d(n)$ pick first $L$ that agrees with evidence through $n$
- Can only fail for sequence $X$ if $X$ keeps showing up in $E(L, n, d(n))$, which happens infinitely often with probability zero (we skipped some details)


## Learnability: [Horning 69]

- Problem: IIL requires that H succeed on each presentation, even the weird ones
- Another criterion: measure one identification
- Assume a distribution $P_{L}(x)$ for each $L$
- Assume $P_{L}(x)$ puts non-zero mass on all and only $x$ in $L$

Assume infinite presentation $X$ drawn i.i.d. from $P_{L}(x)$

- H measure-one identifies $L$ if probability of drawing an $X$ from which H identifies L is 1
- [Horning 69]: PCFGs can be identified in this sense
- Note: there can be misleading sequences, they just have to be (infinitely) unlikely


## Learnability

- Gold's result says little about real learners (requirements of IIL are way too strong)
- Horning's algorithm is completely impractical (needs astronomical amounts of data)
- Even measure-one identification doesn't say anything about tree structures (or even density over strings)
- Only talks about learning grammatical sets
- Strong generative vs weak generative capacity


## Unsupervised Tagging?

- AKA part-of-speech induction
- Task:
- Raw sentences in
- Tagged sentences out
- Obvious thing to do:
- Start with a (mostly) uniform HMM
- Run EM
- Inspect results


## EM for HMMs: Process

- Alternate between recomputing distributions over hidden variables (the tags) and reestimating parameters
- Crucial step: we want to tally up how many (fractional) counts of each kind of transition and emission we have under current params:

$$
\begin{aligned}
& \operatorname{count}(w, s)=\sum_{i: w_{i}=w} P\left(t_{i}=s \mid \mathbf{w}\right) \\
& \operatorname{count}\left(s \rightarrow s^{\prime}\right)=\sum_{i} P\left(t_{i-1}=s, t_{i}=s^{\prime} \mid \mathbf{w}\right)
\end{aligned}
$$

- Same quantities we needed to train a CRF!


## Merialdo: Setup

- Some (discouraging) experiments [Merialdo 94]
- Setup:
- You know the set of allowable tags for each word
- Learn a supervised model on k training sentences
- Learn $\mathrm{P}(\mathrm{w} \mid \mathrm{t})$ on these examples
- Learn $\mathrm{P}\left(\mathrm{t} \mid \mathrm{t}_{-1}, \mathrm{t}_{-2}\right)$ on these examples
- On n > k sentences, re-estimate with EM
- Note: we know allowed tags but not frequencies


## Merialdo: Results

| Number of tagged sentences used for the initial model |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 100 | 2000 | 5000 | 10000 | 20000 | all |
| Iter | Correct tags (\% words) after ML on 1M words |  |  |  |  |  |  |
| 0 | 77.0 | 90.0 | 95.4 | 96.2 | 96.6 | 96.9 | 97.0 |
| 1 | 80.5 | 92.6 | 95.8 | 96.3 | 96.6 | 96.7 | 96.8 |
| 2 | 81.8 | 93.0 | 95.7 | 96.1 | 96.3 | 96.4 | 96.4 |
| 3 | 83.0 | 93.1 | 95.4 | 95.8 | 96.1 | 96.2 | 96.2 |
| 4 | 84.0 | 93.0 | 95.2 | 95.5 | 95.8 | 96.0 | 96.0 |
| 5 | 84.8 | 92.9 | 95.1 | 95.4 | 95.6 | 95.8 | 95.8 |
| 6 | 85.3 | 92.8 | 94.9 | 95.2 | 95.5 | 95.6 | 95.7 |
| 7 | 85.8 | 92.8 | 94.7 | 95.1 | 95.3 | 95.5 | 95.5 |
| 8 | 86.1 | 92.7 | 94.6 | 95.0 | 95.2 | 95.4 | 95.4 |
| 9 | 86.3 | 92.6 | 94.5 | 94.9 | 95.1 | 95.3 | 95.3 |
| 10 | 86.6 | 92.6 | 94.4 | 94.8 | 95.0 | 95.2 | 95.2 |

## Distributional Clustering

- Three main variants on the same idea:
- Pairwise similarities and heuristic clustering
- E.g. [Finch and Chater 92]
- Produces dendrograms
- Vector space methods
- E.g. [Shuetze 93]
- Models of ambiguity
- Probabilistic methods
- Various formulations, e.g. [Lee and Pereira 99]




## Early Approaches: Structure Search

- Incremental grammar learning, chunking [Wolff 88, Langley 82, many others]
- Can recover synthetic grammars
- An (extremely good / lucky) result of incremental structure search:



## Idea: Learn PCFGs with EM

- Classic experiments on learning PCFGs with Expectation-Maximization [Lari and Young, 1990]

$$
\left\{X_{1}, X_{2} \ldots X_{n}\right\}
$$

- Full binary grammar over $n$ symbols

- Parse uniformly/randomly at first
- Re-estimate rule expectations off of parses
- Repeat
- Their conclusion: it doesn't really work.



## Problem: Model Symmetries



- How does this relate to trees



## Other Approaches

- Evaluation: fraction of nodes in gold trees correctly posited in proposed trees (unlabeled recall)
- Some recent work in learning constituency:
- [Adrians, 99] Language grammars aren't general PCFGs
- [Clark, 01] Mutual-information filters detect constituents, then an MDL-guided search assembles them
- [van Zaanen, 00] Finds low edit-distance sentence pairs and extracts their differences


## Right-Branching Baseline

- English trees tend to be right-branching, not balanced

- A simple (English-specific) baseline is to choose the right chain structure for each sentence

| van Zaanen, 00 | 35.6 |
| :--- | :--- | :--- |




## Syntactic Parsing

- Parsing assigns structures to sentences.

- Dependency structure gives attachments.


Idea: Lexical Affinity Models

- Words select other words on syntactic grounds

congress narrowly passed the amended bill
- Link up pairs with high mutual information
- [Yuret, 1998]: Greedy linkage
- [Paskin, 2001]: Iterative re-estimation with EM
- Evaluation: compare linked pairs to a gold standard

| Method | Accuracy |
| :--- | :--- |
| Paskin, 2001 | 39.7 |



## Idea: Word Classes

- Individual words like congress are entwined with semantic facts about the world.
- Syntactic classes, like NOUN and ADVERB are bleached of word-specific semantics.
- Automatic word classes more likely to look like DAYS-OF-WEEK or PERSON-NAME.
- We could build dependency models over word classes. [cf. Carroll and Charniak, 1992]
congress narrowly passed the amended bill



## Results: Dependencies

| Adjacent Words | 55.9 |  |
| :--- | :--- | :--- |
| DMV | 62.7 |  |

- Situation so far:
- Task: unstructured text in, word pairs out
- Previous results were below baseline
- We modeled word classes [cf. Carroll \& Charniak 92]
- We added a model of distance [cf. Collins 99]
- Resulting model is substantially over baseline
- ... but we can do much better

| Results: Combined Models |  |  |
| :--- | :--- | :--- | | Rependency Evaluation (Undir. Dep. Acc.) |  |  |
| :--- | :--- | :--- |
| DMV | 45.6 |  |
| CCM + DMV | 62.7 |  |
| Constituency Evaluation (Unlabeled Recall) |  |  |
| Random 39.4 <br> CCM 81.0 <br> CCM + DMV 88.0 |  |  |
| - Supervised PCFG constituency recall is at 92.8 |  |  |
| - Qualitative improvements |  |  |
| - Subject-verb groups gone, modifier placement improved |  |  |

How General is This?

| English (7422 sentences) Constituency Evaluation  <br> Random Baseline 39.4  <br> CCM+DMV 88.0  <br> German (2175 sentences)   <br> Random Baseline 49.6  <br> CCM+DMV 89.7  <br> Chinese (2473 sentences)  <br> Random Baseline 35.5 <br> CCM+DMV 46.7 <br> DMV 54.2 <br> CCM+DMV 60.0   |  |  |  |
| :--- | :--- | :--- | :---: |

