

# Statistical NLP Spring 2010



## Lecture 21: Compositional Semantics

Dan Klein – UC Berkeley

Includes slides from Luke Zettlemoyer

## Truth-Conditional Semantics

### Linguistic expressions:

- "Bob sings"

### Logical translations:

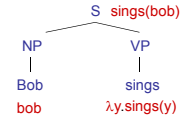
- $sings(bob)$
- Could be  $p_{1218}(e_{397})$

### Denotation:

- $[[bob]] =$  some specific person (in some context)
- $[[sings(bob)]] = ???$

### Types on translations:

- $bob : e$  (for entity)
- $sings(bob) : t$  (for truth-value)



## Truth-Conditional Semantics

### Proper names:

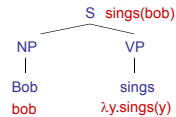
- Refer directly to some entity in the world
- Bob : bob  $[[bob]]^w \rightarrow ???$

### Sentences:

- Are either true or false (given how the world actually is)
- Bob sings :  $sings(bob)$

### So what about verbs (and verb phrases)?

- $sings$  must combine with  $bob$  to produce  $sings(bob)$
- The  $\lambda$ -calculus is a notation for functions whose arguments are not yet filled.
- $sings : \lambda x.sings(x)$
- This is *predicate* – a function which takes an entity (type  $e$ ) and produces a truth value (type  $t$ ). We can write its type as  $e \rightarrow t$ .
- Adjectives?



## Compositional Semantics

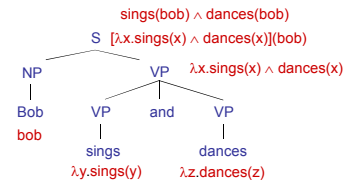
### So now we have meanings for the words

### How do we know how to combine words?

### Associate a combination rule with each grammar rule:

- $S : \beta(\alpha) \rightarrow NP : \alpha \quad VP : \beta$  (function application)
- $VP : \lambda x . \alpha(x) \wedge \beta(x) \rightarrow VP : \alpha$  and  $VP : \beta$  (intersection)

### Example:



## Denotation

### What do we do with logical translations?

- Translation language (logical form) has fewer ambiguities
- Can check truth value against a database
  - Denotation ("evaluation") calculated using the database
- More usefully: assert truth and modify a database
- Questions: check whether a statement in a corpus entails the (question, answer) pair:
  - "Bob sings and dances"  $\rightarrow$  "Who sings?" + "Bob"
- Chain together facts and use them for comprehension

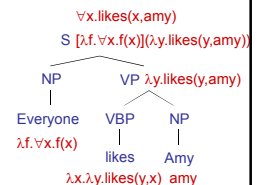
## Other Cases

### Transitive verbs:

- $likes : \lambda x.\lambda y.likes(y,x)$
- Two-place predicates of type  $e \rightarrow (e \rightarrow t)$ .
- $likes\ Amy : \lambda y.likes(y,Amy)$  is just like a one-place predicate.

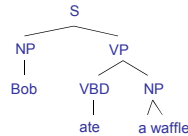
### Quantifiers:

- What does "Everyone" mean here?
- Everyone :  $\lambda f.\forall x.f(x)$
- Mostly works, but some problems
  - Have to change our NP/VP rule.
  - Won't work for "Amy likes everyone."
- "Everyone likes someone."
- This gets tricky quickly!



## Indefinites

- First try
  - "Bob ate a waffle" :  $\text{ate}(\text{bob}, \text{waffle})$
  - "Amy ate a waffle" :  $\text{ate}(\text{amy}, \text{waffle})$
- Can't be right!
  - $\exists x : \text{waffle}(x) \wedge \text{ate}(\text{bob}, x)$
  - What does the translation of "a" have to be?
  - What about "the"?
  - What about "every"?



## Grounding

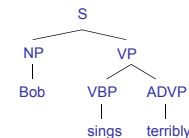
- Grounding
  - So why does the translation  $\text{likes} : \lambda x. \lambda y. \text{likes}(y, x)$  have anything to do with actual liking?
  - It doesn't (unless the denotation model says so)
  - Sometimes that's enough: wire up **bought** to the appropriate entry in a database
- Meaning postulates
  - Insist, e.g.  $\forall x, y. \text{likes}(y, x) \rightarrow \text{knows}(y, x)$
  - This gets into lexical semantics issues
- Statistical version?

## Tense and Events

- In general, you don't get far with verbs as predicates
- Better to have event variables  $e$ 
  - "Alice danced" :  $\text{danced}(\text{alice})$
  - $\exists e : \text{dance}(e) \wedge \text{agent}(e, \text{alice}) \wedge (\text{time}(e) < \text{now})$
- Event variables let you talk about non-trivial tense / aspect structures
  - "Alice had been dancing when Bob sneezed"
  - $\exists e, e' : \text{dance}(e) \wedge \text{agent}(e, \text{alice}) \wedge \text{sneeze}(e') \wedge \text{agent}(e', \text{bob}) \wedge (\text{start}(e) < \text{start}(e') \wedge \text{end}(e) = \text{end}(e')) \wedge (\text{time}(e) < \text{now})$

## Adverbs

- What about adverbs?
  - "Bob sings terribly"
  - $\text{terribly}(\text{sings}(\text{bob}))?$
  - $(\text{terribly}(\text{sings}))(\text{bob})?$
  - $\exists e \text{ present}(e) \wedge \text{type}(e, \text{singing}) \wedge \text{agent}(e, \text{bob}) \wedge \text{manner}(e, \text{terrible})?$
  - Hard to work out correctly!



## Propositional Attitudes

- "Bob thinks that I am a gummi bear"
  - $\text{thinks}(\text{bob}, \text{gummi}(\text{me}))?$
  - $\text{thinks}(\text{bob}, \text{"I am a gummi bear"})?$
  - $\text{thinks}(\text{bob}, \wedge \text{gummi}(\text{me}))?$
- Usual solution involves intensions ( $\wedge X$ ) which are, roughly, the set of possible worlds (or conditions) in which  $X$  is true
- Hard to deal with computationally
  - Modeling other agents models, etc
  - Can come up in simple dialog scenarios, e.g., if you want to talk about what your bill claims you bought vs. what you actually bought

## Trickier Stuff

- Non-Intersective Adjectives
  - $\text{green ball} : \lambda x. [\text{green}(x) \wedge \text{ball}(x)]$
  - $\text{fake diamond} : \lambda x. [\text{fake}(x) \wedge \text{diamond}(x)] ? \rightarrow \lambda x. [\text{fake}(\text{diamond}(x))]$
- Generalized Quantifiers
  - $\text{the} : \lambda f. [\text{unique-member}(f)]$
  - $\text{all} : \lambda f. \lambda g. [\forall x. f(x) \rightarrow g(x)]$
  - $\text{most}?$
  - Could do with more general second order predicates, too (why worse?)
    - $\text{the}(\text{cat}, \text{meows}), \text{all}(\text{cat}, \text{meows})$
- Generics
  - "Cats like naps"
  - "The players scored a goal"
- Pronouns (and bound anaphora)
  - "If you have a dime, put it in the meter."
- ... the list goes on and on!

## Multiple Quantifiers

- Quantifier scope
  - Groucho Marx celebrates quantifier order ambiguity:
    - "In this country a woman gives birth every 15 min.
    - Our job is to find that woman and stop her."
- Deciding between readings
  - "Bob bought a pumpkin every Halloween"
  - "Bob put a warning in every window"
  - Multiple ways to work this out
    - Make it syntactic (movement)
    - Make it lexical (type-shifting)

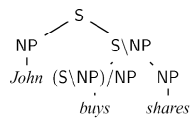
## Modeling Uncertainty?

- Gaping hole warning!
- Big difference between statistical disambiguation and statistical reasoning.
  - The scout saw the enemy soldiers with night goggles.*
    - With probabilistic parsers, can say things like "72% belief that the PP attaches to the NP."
    - That means that *probably* the enemy has night vision goggles.
    - However, you can't throw a logical assertion into a theorem prover with 72% confidence.
    - Not clear humans really extract and process logical statements symbolically anyway.
    - Use this to decide the expected utility of calling reinforcements?
- In short, we need probabilistic reasoning, not just probabilistic disambiguation followed by symbolic reasoning!

## CCG Parsing

- Combinatory  
Categorial  
Grammar
  - Fully (mono-) lexicalized grammar
  - Categories encode argument sequences
  - Very closely related to the lambda calculus
  - Can have spurious ambiguities (why?)

$John \vdash NP : john'$   
 $shares \vdash NP : shares'$   
 $buys \vdash (S \setminus NP) / NP : \lambda x. \lambda y. buys' xy$   
 $sleeps \vdash S \setminus NP : \lambda x. sleeps' x$   
 $well \vdash (S \setminus NP) \setminus (S \setminus NP) : \lambda f. \lambda x. well''(fx)$



## Mapping to Logical Form

- Learning to Map Sentences to Logical Form

Texas borders Kansas



$borders(texas, kansas)$

## Some Training Examples

Input: What states border Texas?  
 Output:  $\lambda x. state(x) \wedge borders(x, texas)$

Input: What is the largest state?  
 Output:  $argmax(\lambda x. state(x), \lambda x. size(x))$

Input: What states border the largest state?  
 Output:  $\lambda x. state(x) \wedge borders(x, argmax(\lambda y. state(y), \lambda y. size(y)))$

## CCG Lexicon

Words	Category
	Syntax : Semantics
Texas	NP : $texas$
borders	$(S \setminus NP) / NP : \lambda x. \lambda y. borders(y, x)$
Kansas	NP : $kansas$
Kansas city	NP : $kansas\_city\_MO$

## Parsing Rules (Combinators)

- Application

▪  $X/Y : f \quad Y : a \Rightarrow X : f(a)$

$(S \backslash NP) / NP \quad NP \quad S \backslash NP$   
 $\lambda x. \lambda y. borders(y, x) \quad texas \quad \lambda y. borders(y, texas)$

▪  $Y : a \quad X \backslash Y : f \Rightarrow X : f(a)$

$NP \quad S \backslash NP \quad S$   
 $kansas \quad \lambda y. borders(y, texas) \quad borders(kansas, texas)$

- Additional rules

- Composition
- Type Raising

## CCG Parsing

Texas	borders	Kansas
NP	$(S \backslash NP) / NP$	NP
texas	$\lambda x. \lambda y. borders(y, x)$	kansas
$S \backslash NP$		
$\lambda y. borders(y, kansas)$		
S		
$borders(texas, kansas)$		

## Parsing a Question

What	states	border	Texas
$S / (S \backslash NP) / N$	N	$(S \backslash NP) / NP$	NP
$\lambda f. \lambda g. \lambda x. f(x) \wedge g(x)$	$\lambda x. state(x)$	$\lambda x. \lambda y. borders(y, x)$	texas
$S / (S \backslash NP)$		$S \backslash NP$	
$\lambda g. \lambda x. state(x) \wedge g(x)$		$\lambda y. borders(y, texas)$	
S			
$\lambda x. state(x) \wedge borders(x, texas)$			

## Lexical Generation

### Input Training Example

Sentence: Texas borders Kansas  
 Logic Form:  $borders(texas, kansas)$

### Output Lexicon

Words	Category
Texas	NP : texas
borders	$(S \backslash NP) / NP : \lambda x. \lambda y. borders(y, x)$
Kansas	NP : kansas
...	...

## GENLEX

- Input: a training example  $(S_i, L_i)$
- Computation:
  - Create all substrings of words in  $S_i$
  - Create categories from  $L_i$
  - Create lexical entries that are the cross product of these two sets
- Output: Lexicon  $\Delta$

## GENLEX Cross Product

### Input Training Example

Sentence: Texas borders Kansas  
 Logic Form:  $borders(texas, kansas)$

### Output Lexicon

<ul style="list-style-type: none"> <li>Output Substrings:</li> <li>Texas</li> <li>borders</li> <li>Kansas</li> <li>Texas borders</li> <li>borders Kansas</li> <li>Texas borders Kansas</li> </ul>	X	<ul style="list-style-type: none"> <li>Output Categories:</li> <li>NP : texas</li> <li>NP : kansas</li> <li><math>(S \backslash NP) / NP : \lambda x. \lambda y. borders(y, x)</math></li> </ul>
---	---	--

GENLEX is the cross product in these two output sets

## GENLEX: Output Lexicon

Words	Category
Texas	NP : <i>texas</i>
Texas	NP : <i>kansas</i>
Texas	(S\NP)/NP : $\lambda x.\lambda y.borders(y,x)$
borders	NP : <i>texas</i>
borders	NP : <i>kansas</i>
borders	(S\NP)/NP : $\lambda x.\lambda y.borders(y,x)$
...	...
Texas borders Kansas	NP : <i>texas</i>
Texas borders Kansas	NP : <i>kansas</i>
Texas borders Kansas	(S\NP)/NP : $\lambda x.\lambda y.borders(y,x)$

## Weighted CCG

Given a log-linear model with a CCG lexicon  $\Lambda$ , a feature vector  $f$ , and weights  $w$ .

The best parse is:

$$y^* = \underset{y}{\operatorname{argmax}} w \cdot f(x,y)$$

Where we consider all possible parses  $y$  for the sentence  $x$  given the lexicon  $\Lambda$ .

**Inputs:** Training set  $\{(x_i, z_i) \mid i=1..n\}$  of sentences and logical forms. Initial lexicon  $\Lambda$ . Initial parameters  $w$ . Number of iterations  $T$ .

**Computation:** For  $t = 1..T, i = 1..n$ :

Step 1: Check Correctness

- Let  $y^* = \underset{y}{\operatorname{argmax}} w \cdot f(x_i, y)$
- If  $L(y^*) = z_i$ , go to the next example

Step 2: Lexical Generation

- Set  $\lambda = \Lambda \cup \text{GENLEX}(x_i, z_i)$
- Let  $\hat{y} = \underset{y \text{ s.t. } L(y)=z_i}{\operatorname{argmax}} w \cdot f(x_i, y)$
- Define  $\lambda_i$  to be the lexical entries in  $\hat{y}$
- Set lexicon to  $\Lambda = \Lambda \cup \lambda_i$

Step 3: Update Parameters

- Let  $y' = \underset{y}{\operatorname{argmax}} w \cdot f(x_i, y)$
- If  $L(y') \neq z_i$ 
  - Set  $w = w + f(x_i, \hat{y}) - f(x_i, y')$

**Output:** Lexicon  $\Lambda$  and parameters  $w$ .

## Example Learned Lexical Entries

Words	Category
states	N : $\lambda x.state(x)$
major	N/N : $\lambda g.\lambda x.major(x) \wedge g(x)$
population	N : $\lambda x.population(x)$
cities	N : $\lambda x.city(x)$
river	N : $\lambda x.river(x)$
run through	(S\NP)/NP : $\lambda x.\lambda y.traverse(y,x)$
the largest	NP/N : $\lambda g.\operatorname{argmax}(g, \lambda x.size(x))$
rivers	N : $\lambda x.river(x)$
the highest	NP/N : $\lambda g.\operatorname{argmax}(g, \lambda x.elev(x))$
the longest	NP/N : $\lambda g.\operatorname{argmax}(g, \lambda x.len(x))$
...	...

## Challenge Revisited

The lexical entries that work for:

Show me the latest flight from Boston to Prague on Friday

S\NP    NP/N    N    N\N    N\N    N\N

Will not parse:

Boston to Prague the latest on Friday

NP    N\N    NP/N    N\N

## Disharmonic Application

Reverse the direction of the principal category:

X\Y : f    Y : a    =>    X : f(a)  
 Y : a    X/Y : f    =>    X : f(a)

flights	one way
N	N/N
$\lambda x.flight(x)$	$\lambda f.\lambda x.f(x) \wedge one\_way(x)$
N	
$\lambda x.flight(x) \wedge one\_way(x)$	

## Missing content words

### Insert missing semantic content

$NP : c \Rightarrow N \setminus N : \lambda f. \lambda x. f(x) \wedge p(x, c)$

<b>flights</b>	<b>Boston</b>	<b>to Prague</b>
$N$	$NP$	$N \setminus N$
$\lambda x. flight(x)$	$BOS$	$\lambda f. \lambda x. f(x) \wedge to(x, PRG)$
	$N \setminus N$	
	$\lambda f. \lambda x. f(x) \wedge from(x, BOS)$	
	$N$	
	$\lambda x. flight(x) \wedge from(x, BOS)$	
	$N$	
	$\lambda x. flight(x) \wedge from(x, BOS) \wedge to(x, PRG)$	

## Missing content-free words

### Bypass missing nouns

$N \setminus N : f \Rightarrow N : f(\lambda x. true)$

<b>Northwest Air</b>	<b>to Prague</b>
$N \setminus N$	$N \setminus N$
$\lambda f. \lambda x. f(x) \wedge airline(x, NWA)$	$\lambda f. \lambda x. f(x) \wedge to(x, PRG)$
	$N$
	$\lambda x. to(x, PRG)$
	$N$
	$\lambda x. airline(x, NWA) \wedge to(x, PRG)$

## A Complete Parse

<b>Boston</b>	<b>to Prague</b>	<b>the latest</b>	<b>on Friday</b>
$NP$	$N \setminus N$	$NP \setminus N$	$N \setminus N$
$BOS$	$\lambda f. \lambda x. f(x) \wedge to(x, PRG)$	$\lambda f. argmax(\lambda x. f(x), \lambda x. time(x))$	$\lambda f. \lambda x. f(x) \wedge day(x, FRI)$
	$N \setminus N$		$N$
	$\lambda f. \lambda x. f(x) \wedge from(x, BOS)$		$\lambda x. day(x, FRI)$
	$N \setminus N$		
	$\lambda f. \lambda x. f(x) \wedge from(x, BOS) \wedge to(x, PRG)$		
	$NP \setminus N$		
	$\lambda f. argmax(\lambda x. f(x) \wedge from(x, BOS) \wedge to(x, PRG), \lambda x. time(x))$		
		$N$	
		$argmax(\lambda x. from(x, BOS) \wedge to(x, PRG) \wedge day(x, FRI), \lambda x. time(x))$	

## Geo880 Test Set

Exact Match Accuracy:	Precision	Recall	F1
Zettlemoyer & Collins 2007	95.49	83.20	88.93
Zettlemoyer & Collins 2005	96.25	79.29	86.95
Wong & Money 2007	93.72	80.00	86.31