## CS 294-5: Statistical Natural Language Processing



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## Last Time

- Maximum entropy models
- A technique for estimating multinomial distributions conditionally on many features

$$
P(c \mid d, \lambda)=\frac{\exp \sum_{i} \lambda_{i}(c) f_{i}(d)}{\sum_{c^{\prime}} \exp \sum_{i} \lambda_{i}(c) f_{i}(d)}
$$

- A building block of many NLP systems
- Catch-up session on Wednesday!
- (a) First part of my office hours (3-4)
- (b) Right before my office hours (2-3)

|  | Parts-of | oeech |
| :---: | :---: | :---: |
| - Syntactic classes of words <br> - Useful distinctions vary from language to language <br> - Tagsets vary from corpus to corpus [See M+S p. 142] |  |  |
| Some tags from the Penn tagset |  |  |
| CD DT | numeral, cardinal determiner | mid-1890 nine-thirty 0.5 one |
| DT IN | determiner preposition or conjunction, subordinating | a all an every no that the among whether out on by if |
| JJ | adjective or numeral, ordinal | third ill-mannered regrettable |
| MD | modal auxiliary | can may might will would |
| NN | noun, common, singular or mass | cabbage thermostat investment subhumanity |
| NNP | noun, proper, singular | Motown Cougar Yvette Liverpool |
| PRP | pronoun, personal | hers himself it we them |
| RB | adverb | occasionally maddeningly adventurously |
| RP | particle | aboard away back by on open through |
| VB | verb, base form | ask bring fire see take |
| vbd | verb, past tense | pleaded swiped registered saw |
| vbs | verb, past participle | dilapidated imitated reunifed unsettled |
| vBP | verb, present tense, not 3rd person singular | twist appear comprise mold postpone |

## Part-of-Speech Ambiguity

- Example

| VBD |  | VB |  |  |
| :--- | :--- | :---: | :---: | :---: |
| VBN | VBZ | VBP | VBZ |  |
| NNP | NNS | NN | NNS | $C D$ |$\quad$ NN

- Two basic sources of constraint:
- Grammatical environment
- Identity of the current word
- Many more possible features:
- ... but we won't be able to use them until next class


## Why POS Tagging?

- Useful in and of itself
- Text-to-speech: record, lead
- Lemmatization: saw[v] $\rightarrow$ see, saw[n] $\rightarrow$ saw
- Quick-and-dirty NP-chunk detection: grep \{JJ | NN\} ${ }^{\star}$ \{NN | NNS\}
- Useful as a pre-processing step for parsing
- Less tag ambiguity means fewer parses
- However, some tag choices are better decided by parsers!

> DT NNP NN VBD VBN RP NN NNS

The Georgia branch had taken on loan commitments .

## HMMs

- We want a generative model over sequences $t$ and observations $w$ using states s

$$
P(T, W)=\prod P\left(t_{i} \mid t_{i-1}, t_{i-2}\right) P\left(w_{i} \mid t_{i}\right)
$$

$$
P(T, W)=\prod P\left(s_{i} \mid s_{i-1}\right) P\left(w_{i} \mid s_{i}\right)
$$



- Assumptions:
- Tag sequence is generated by an order n markov model

This corresponds to a $1^{\text {st }}$ order model over tag n -grams

- Words are chosen independently, conditioned only on the tag
- These are totally broken assumptions: why?

Parameter Estimation

- Need two multinomials
- Transitions:

$$
P\left(t_{i} \mid t_{i-1}, t_{i-2}\right)
$$

- Emissions:
$P\left(w_{i} \mid t_{i}\right)$
- Can get these off a collection of tagged sentences:
- [examples]


## Practical Issues with Estimation

- Use standard smoothing methods to estimate transition scores, e.g.:

$$
P\left(t_{i} \mid t_{i-1}, t_{i-2}\right)=\lambda_{2} \hat{P}\left(t_{i} \mid t_{i-1}, t_{i-2}\right)+\lambda_{1} \hat{P}\left(t_{i} \mid t_{i-1}\right)
$$

- Emissions are tricker
- Words we've never seen before
- Words which occur with tags we've never seen
- One option: break out the Good-Turning smoothing
- Issue: words aren't black boxes:

$$
\text { 343,127.23 11-year } \quad \text { Minteria } \quad \text { reintroducible }
$$

- Another option: decompose words into features and use a maxent model along with Bayes' rule.

$$
P(w \mid t)=P_{\text {MAXENT }}(t \mid w) P(w) / P(t)
$$

## Disambiguation

- Given these two multinomials, we can score any word / tag sequence pair

NNP VBZ NN NNS CD NN Fed raises interest rates 0.5 percent
$P(N N P \mid<\star, \star>) P($ Fed $\mid N N P) P(V B Z \mid<N N P, \bullet>) P($ raises $\mid V B Z) P(N N \mid V B Z, N N P) \ldots$
- In principle, we're done - list all possible tag sequences, score each one, pick the best one (the Viterbi state sequence)

| NNP VBZ NN NNS CD NN |  |  |  |  | $\log \mathrm{P}=-23$ |
| :--- | :--- | :--- | :---: | :---: | :---: |
| NNP NNS NN NNS CD NN | $\Rightarrow$ | $\log \mathrm{P}=-29$ |  |  |  |
| NNP VBZ VB NNS CD NN |  | $\log \mathrm{P}=-27$ |  |  |  |

NNP VBZ NN NNS CD NN $\Rightarrow \quad \log P=-23$

NNP VBZ VB NNS CD NN $\Rightarrow \quad \log P=-27$

## Finding the Best Trajectory

- Too many trajectories (state sequences) to list
- Option 1: Beam Search

$$
<>\xrightarrow{\text { Fed:NNP }} \text { Fed:VBN Fed:NNP raises:NNS } \xrightarrow{\longrightarrow} \xrightarrow{\longrightarrow}
$$

- A beam is a set of partial hypotheses
- Start with just the single empty trajectory
- At each derivation step:

Consider all continuations of previous hypotheses
Discard most, keep top k, or those within a factor of the best, (or some combination)

- Beam search works relatively well in practice
- ... but sometimes you want the optimal answer
- ... and you need optimal answers to validate your beam search


## The Path Trellis

- Represent paths as a trellis over states

- Each arc $\left(\mathrm{s}_{1}: i \rightarrow \mathrm{~s}_{2}: i+1\right)$ is weighted with the combined cost of: - Transitioning from $\mathrm{s}_{1}$ to $\mathrm{s}_{2}$ (which involves some unique tag t ) - Emitting word i given t

P(VBZ | NNP, •) P(raises | VBZ)

- Each state path (trajectory):
- Corresponds to a derivation of the word and tag sequence pair
- Corresponds to a unique sequence of part-of-speech tags
- Has a probability given by multiplying the arc weights in the path


## The Viterbi Algorithm

- Dynamic program for computing

$$
\delta_{i}(s)=\max _{s_{0} \ldots s_{i-1} s} P\left(s_{0} \ldots s_{i-1} s, w_{1} \ldots w_{i}\right)
$$

- The score of a best path up to position i ending in state $s$

$$
\begin{aligned}
& \delta_{0}(s)=\left\{\begin{array}{lc}
1 & \text { if } s=\langle\bullet, \bullet\rangle \\
0 & \text { otherwise }
\end{array}\right. \\
& \delta_{i}(s)=\max _{s^{\prime}} P\left(s \mid s^{\prime}\right) P(w \mid s) \delta_{i-1}\left(s^{\prime}\right)
\end{aligned}
$$

- Also store a backtrace

$$
\psi_{i}(s)=\underset{c^{\prime}}{\arg \max } P\left(s \mid s^{\prime}\right) P(w \mid s) \delta_{i-1}\left(s^{\prime}\right)
$$

- Memoized solution
- Iterative solution


## So How Does It Work?

- Choose the most common tag
- $90.3 \%$ with a bad unknown word model
- $93.7 \%$ with a good one!
- TnT (Brants, 2000):
- A carefully smoothed trigram tagger
- $96.7 \%$ on WSJ text (SOA is $\sim 97.2 \%$ )
- Noise in the data
- Many errors in the training and test corpora

DT NN IN NN VBD NNS VBD The average of interbank offered rates plummeted

- Probably about $2 \%$ guaranteed error from noise (on this data)

JJ JJ NN chief executive officer
NN JJ NN chief executive officer JJ NN NN chief executive officer NN
chief executive officer

## What's Next for POS Tagging

- Better features!

$$
\begin{aligned}
& \text { RB } \\
& \text { PRP VBD IN RB IN PRP VBD } \\
& \text { They left as soon as he arrived. }
\end{aligned}
$$

- We could fix this with a feature that looked at the next word


NNP NNS VBD VBN
Intrinsic flaws remained undetected

- We could fix this by linking capitalized words to their lowercase versions
- Solution: maximum entropy sequence models (next class)
- Reality check:
- Taggers are already pretty good on WSJ journal text...
- What the world needs is taggers that work on other text!


## HMMs as Language Models

- We have a generative model of tagged sentences:

$$
P(T, W)=\prod_{i} P\left(t_{i} \mid t_{i-1}, t_{i-2}\right) P\left(w_{i} \mid t_{i}\right)
$$

- We can turn this into a distribution over sentences by summing over the tag sequences:

$$
P(W)=\sum_{T} \prod_{i} P\left(t_{i} \mid t_{i-1}, t_{i-2}\right) P\left(w_{i} \mid t_{i}\right)
$$

- Problem: too many sequences!
- (And beam search isn't going to help this time)


## Summing over Paths

- Just like Viterbi, but with sum instead of max

$$
\begin{aligned}
& \delta_{i}(s)=\max _{s_{0} \ldots s_{i-1} s} P\left(s_{0} \ldots s_{i-1} s, w_{1} \ldots w_{i}\right) \\
& \alpha_{i}(s)=\sum_{s_{0} \ldots w_{i-1} s} P\left(s_{0} \ldots s_{i-1} s, w_{1} \ldots w_{i}\right)
\end{aligned}
$$

- Recursive decomposition
$\alpha_{0}(s)=\left\{\begin{array}{lc}1 & \text { if } s=\langle\bullet, \bullet\rangle \\ 0 & \text { otherwise }\end{array}\right.$
$\alpha_{i}(s)=\sum_{s^{\prime}} P\left(s \mid s^{\prime}\right) P(w \mid s) \alpha_{i-1}\left(s^{\prime}\right)$

The Forward-Backward Algorithm

$$
\begin{aligned}
& \alpha_{i}(s)=\sum_{s_{0}, s_{1-1} s} P\left(s_{0} \ldots s_{i-1} s, w_{1} \ldots w_{i}\right) \\
& \beta_{i}(s)=\sum_{s_{i}+1, \ldots s_{n}} P\left(s_{i+1} \ldots s_{n}, w_{i+1} \ldots w_{n} \mid s\right)
\end{aligned}
$$

## How's the HMM as a LM?

- POS tagging HMMs are terrible as LMs!

I bought an ice cream __
The computer that I set up yesterday just ___

- Don't capture long-distance effects like a parser could
- Don't capture local collocational effects like n-grams
- But other HMM-based LMs can work very well



## What Does This Buy Us?

- Why do we want forward and backward probabilities?
- Lets us ask more questions
- Like: what fraction of sequences contain tag t at position i

$$
\gamma_{i}\left(s, s^{\prime}\right)=\alpha_{i-1}(s) P\left(s^{\prime} \mid s\right) P\left(w_{i} \mid s^{\prime}\right) \beta_{i}\left(s^{\prime}\right)
$$

$$
P\left(t_{i}=t \mid w_{1} \ldots w_{n}\right)=\frac{\sum_{s \rightarrow s^{\prime}: \operatorname{tag}\left(s^{\prime}\right)=t_{i}} \gamma_{i}\left(s, s^{\prime}\right)}{\sum_{s \rightarrow s^{\prime}} \gamma_{i}\left(s, s^{\prime}\right)}
$$

- Max-tag decoding:
- Pick the tag at each point which has highest expectation
- Raises accuracy a tiny bit
- Bad idea in practice (why?)
- Also: Unsupervised learning of HMMs
- At least in theory, more later.


## Next Time

- Better Tagging Features using Maxent
- Dealing with unknown words
- Adjacent words
- Longer-distance features
- Named-Entity Recognition
- Reading: M+S 9-10, J+M 7.1-7.4

