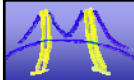
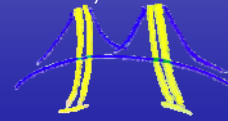


Engineering Parallel Software with Our Pattern Language

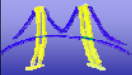
Professor Kurt Keutzer and Tim Mattson
and
(Jake Chong), Ekaterina Gonina, Bor-Yiing Su
and
Michael Anderson, Bryan Catanzaro,
Chao-Yue Lai, Mark Murphy, David Sheffield,
Naryanan Sundaram,



Main Points of Previous Lecture

- ❖ Many approaches to parallelizing software are *not* working
 - Profile and improve
 - Swap in a new parallel programming language
 - Rely on a super parallelizing compiler
- ❖ My own experience has shown that a sound software architecture is the greatest single indicator of a software project's success.
- ❖ Software must be **architected** to achieve productivity, efficiency, and correctness
- ❖ SW architecture >> programming environments
 - >> programming languages
 - >> compilers and debuggers
 - (>>hardware architecture)
- ❖ If we had understood how to architect sequential software, then parallelizing software would not have been such a challenge
- ❖ Key to **architecture** (software or otherwise) is **design patterns** and a **pattern language**
- ❖ At the highest level our pattern language has:
 - Eight structural patterns
 - Thirteen computational patterns
- ❖ Yes, we really believe arbitrarily complex parallel software can built just from these!

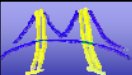
2/77



Outline

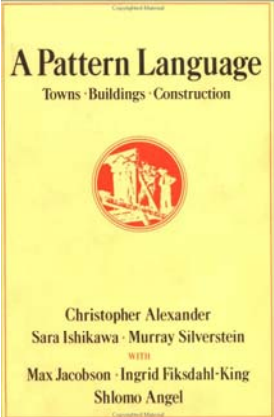
- ➔ ■ Our Pattern Language for parallel programming
 - Detailed example using Our Pattern Language

3/77

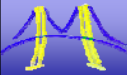


Alexander's Pattern Language

- ❖ Christopher Alexander's approach to (civil) architecture:
 - "Each **pattern** describes a problem which occurs over and over again in our environment, and then describes the core of the solution to that problem, in such a way that you can use this solution a million times over, without ever doing it the same way twice." *Page x, A Pattern Language, Christopher Alexander*
- ❖ Alexander's 253 (civil) architectural **patterns** range from the creation of cities (2. distribution of towns) to particular building problems (232. roof cap)
- ❖ A **pattern language** is an organized way of tackling an architectural problem using patterns
- ❖ Main limitation:
 - It's about civil not software architecture!!!



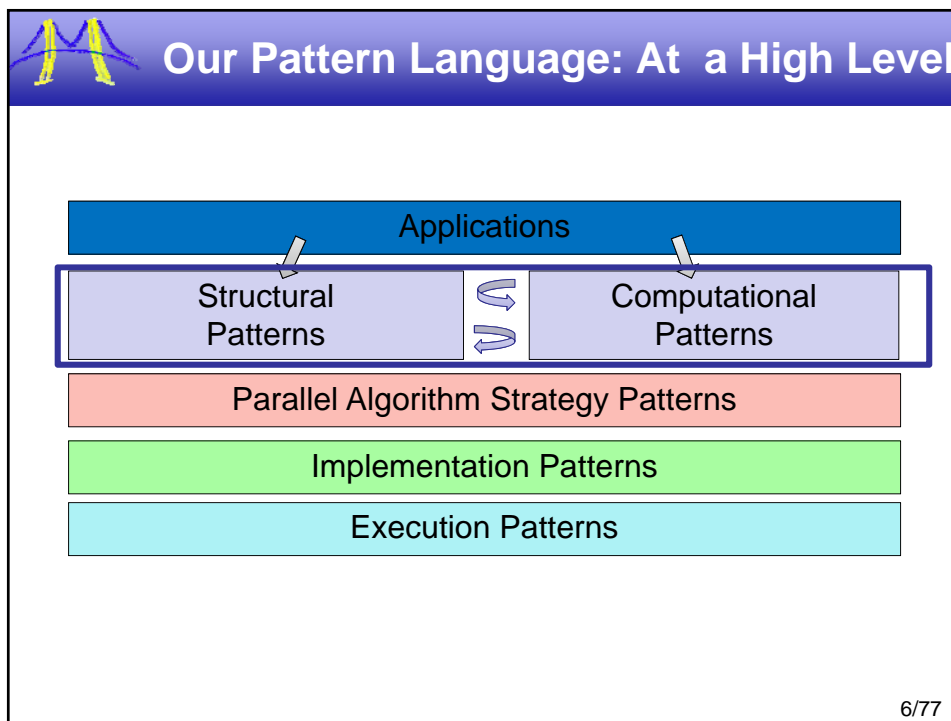
4
4/77

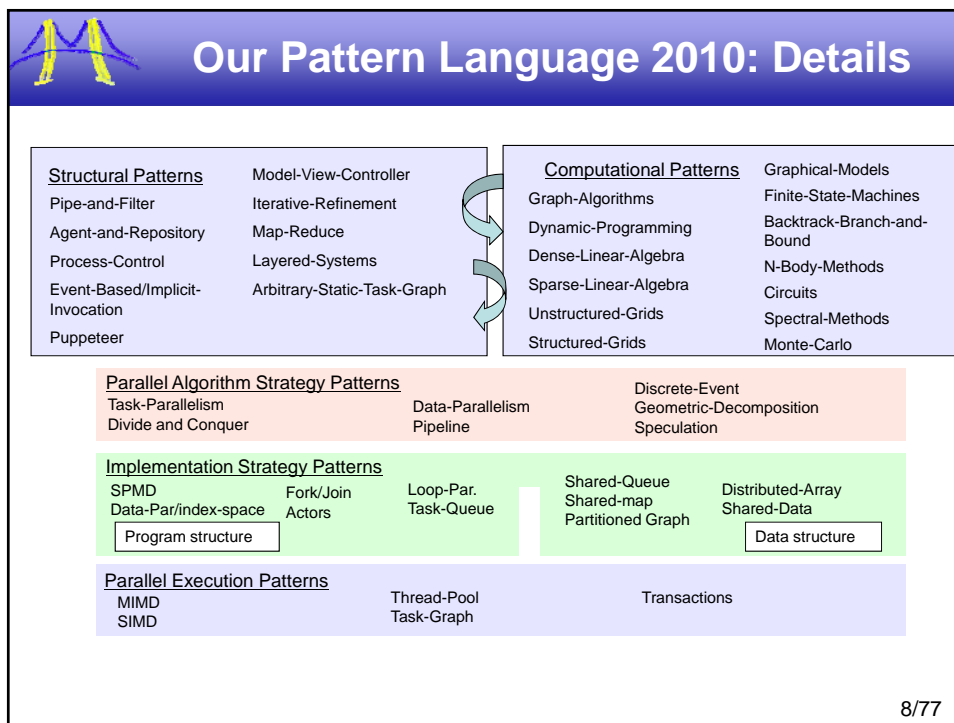
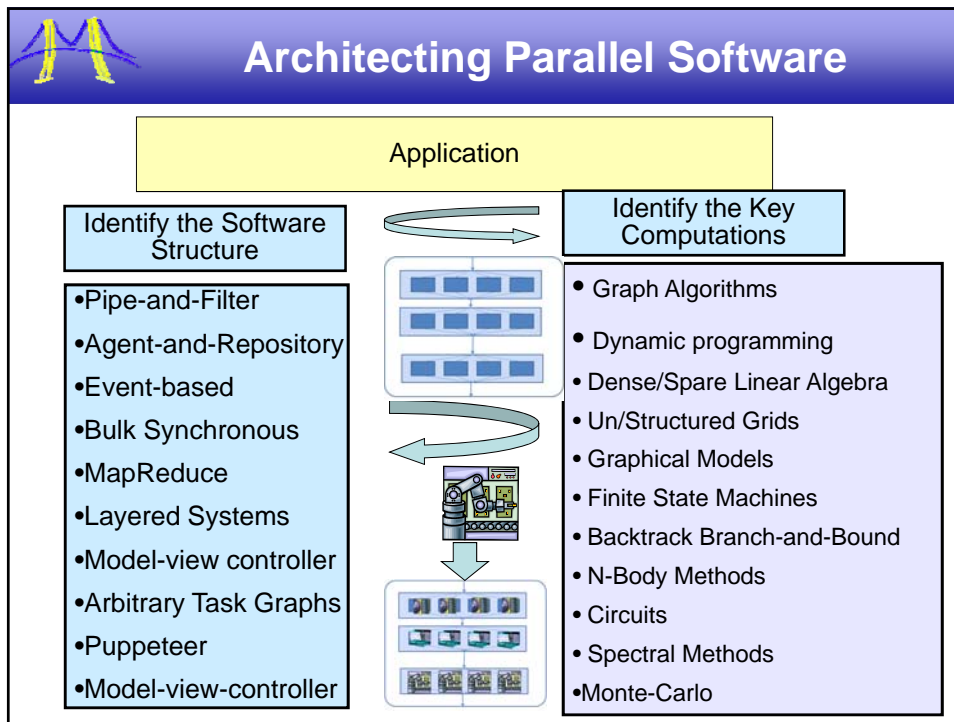


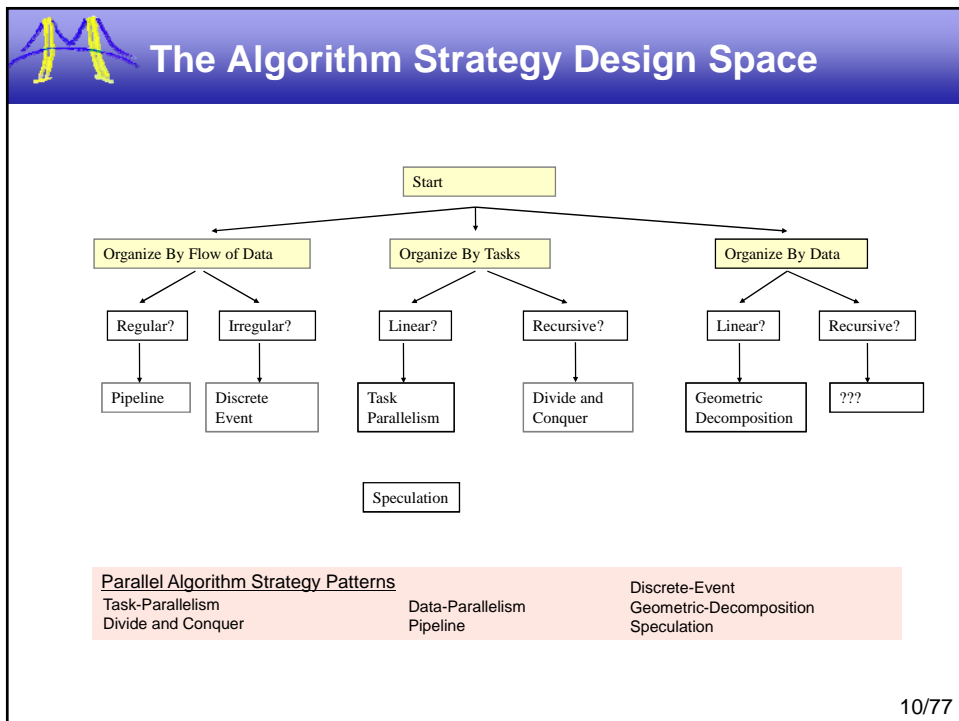
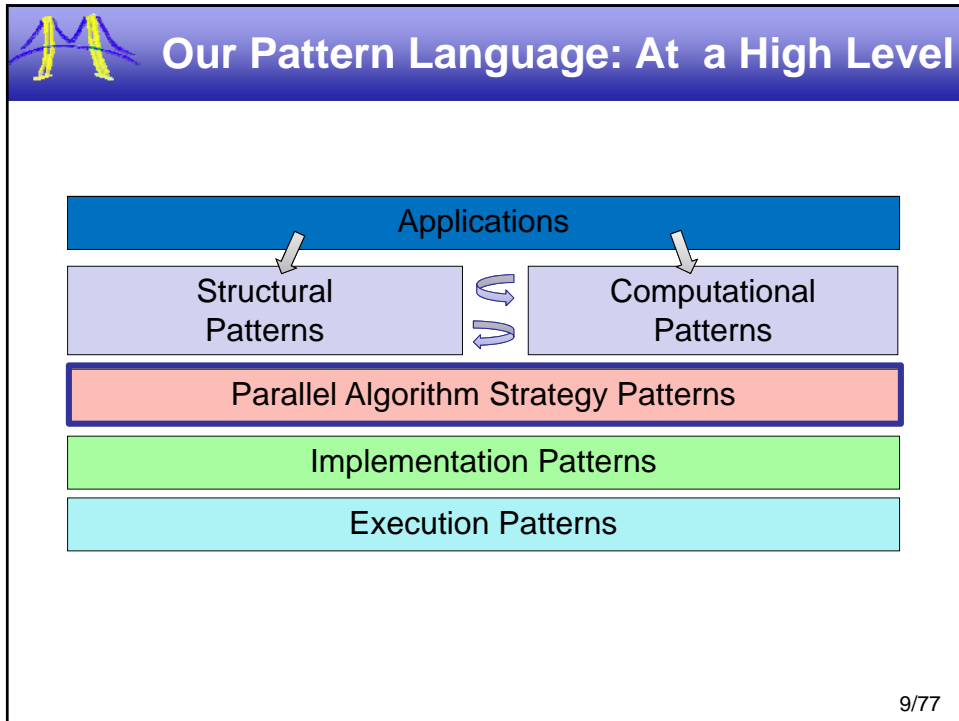
A Pattern Language

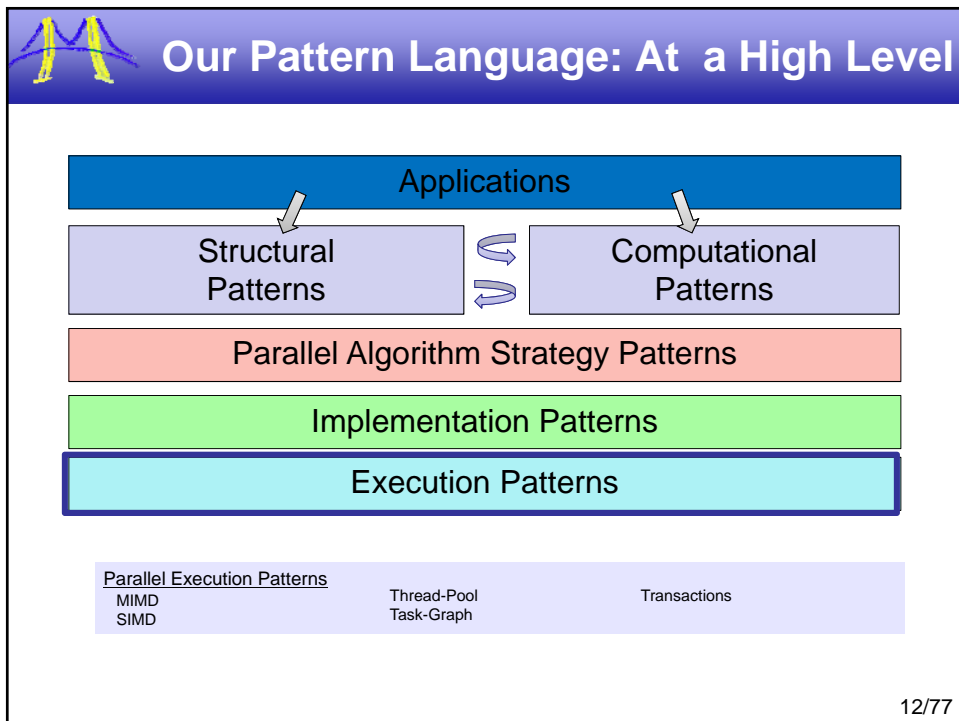
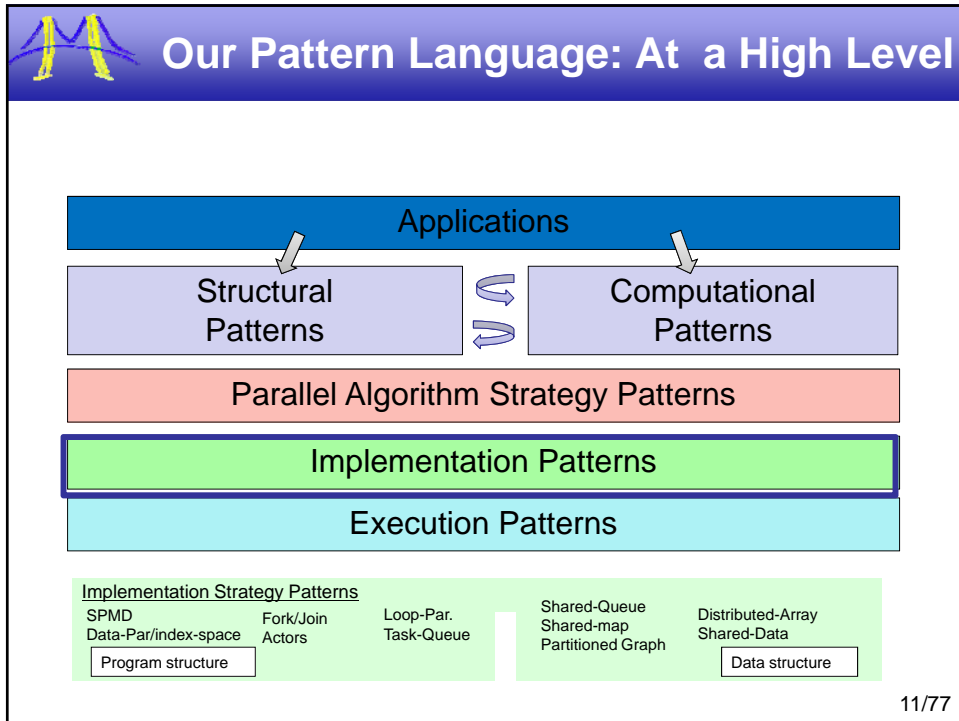
- *Patterns* embody generalizable solutions to recurrent problems
- Collections of individual patterns (e.g. *Design Patterns*, Gamma, Helm, Johnson, Vlissides) are great, but we need more help in the software development enterprise
- We would like a comprehensive *pattern language* which covers the entire process of parallel software development and implementation
- Keutzer, Mattson, the PALLAS group, and others have developed just such a pattern language
 - <http://parlab.eecs.berkeley.edu/wiki/patterns>
- Pattern language is overviewed in:
 - http://parlab.eecs.berkeley.edu/wiki/_media/patterns/opl-new_with_appendix-20091014.pdf
- Today we don't have time to go through all the patterns, but we will briefly describe the structure of OPL and show how it can be used

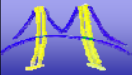
5/77







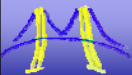




Outline

- Our Pattern Language for parallel programming
- ■ Detailed example using Our Pattern Language

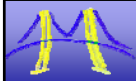
13/77



Outline

- **Speech Recognition Application**
 - Software Architecture using Patterns
 - Identify Structural Patterns
 - Identify Computational Patterns
 - Parallelization: (for each module)
 - Algorithm strategy pattern
 - Implementation strategy pattern
 - Execution patterns
 - Conclusion

14/77

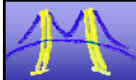


Automatic Speech Recognition

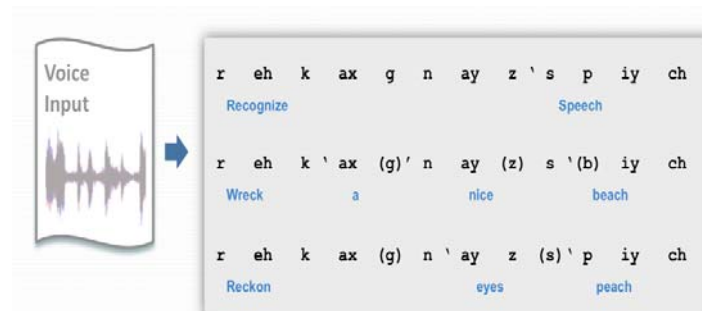
- Key technology for enabling rich human-computer interaction
 - Increasingly important for intelligent devices without keyboards
- Interaction requires low latency responses
 - Only one of many components in exciting new real-time applications
- Main contributions:
 - A detailed analysis of the concurrency in large vocabulary continuous speech recognition (LVCSR) summarized in the pattern language
 - An implementation on GPU with **11x** speedup over optimized C++ version
 - Achieving **3x** better than real time performance with 50,000 word vocabulary



15/77

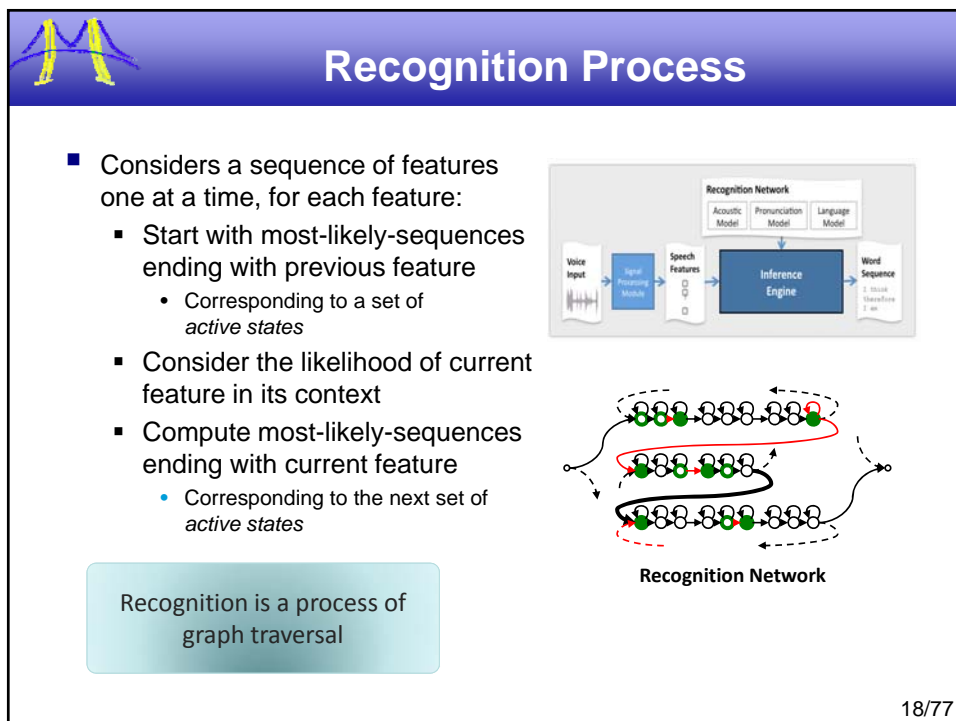
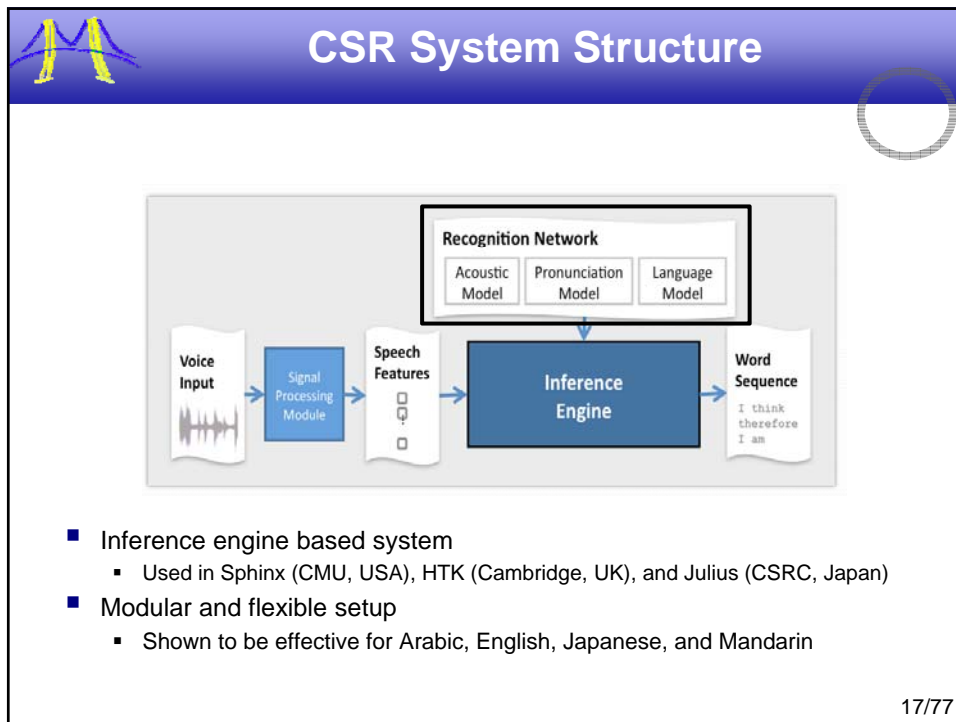


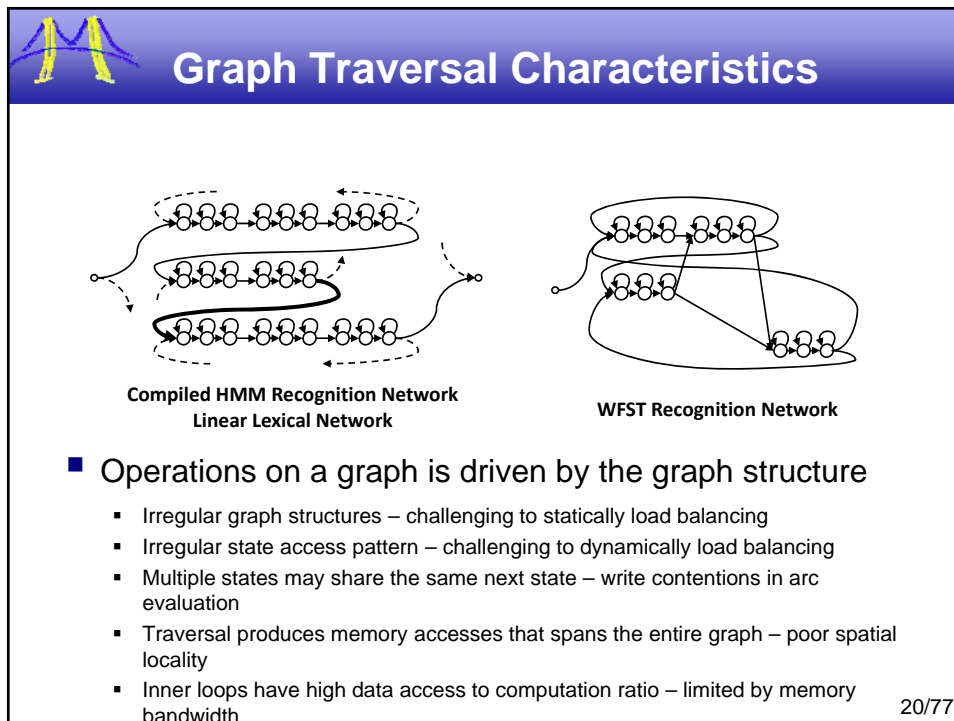
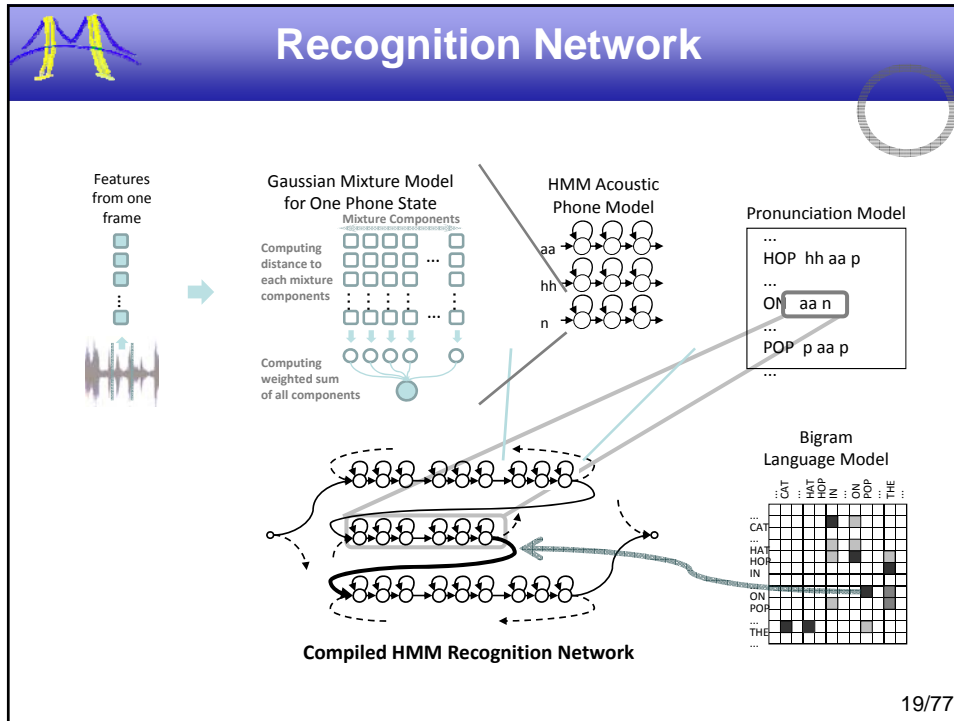
Continuous Speech Recognition



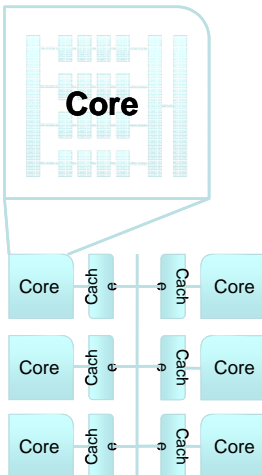
- Challenges:
 - Recognizing words from a large vocabulary arranged in exponentially many possible permutations
 - Inferring word boundaries from the context of neighboring words
- Hidden Markov Model (HMM) is the most successful approach

16/77





Parallel Platform Characteristics



The diagram illustrates a parallel platform architecture. At the top left, a callout box labeled 'Core' shows a grid of vertical bars representing a core's internal structure. Below this, a larger diagram shows a 3x2 grid of 'Core' blocks. Each 'Core' block is connected to a 'Cach' (cache) block. The caches are arranged in a central vertical column, with each core connected to its adjacent cache. This represents a shared cache architecture for multiple cores.

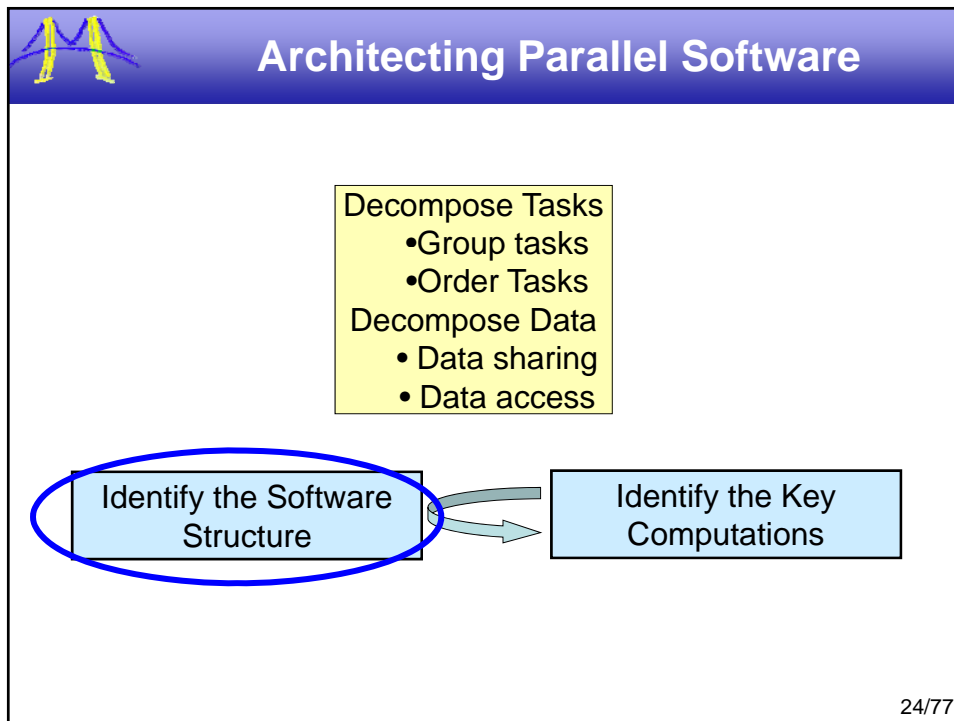
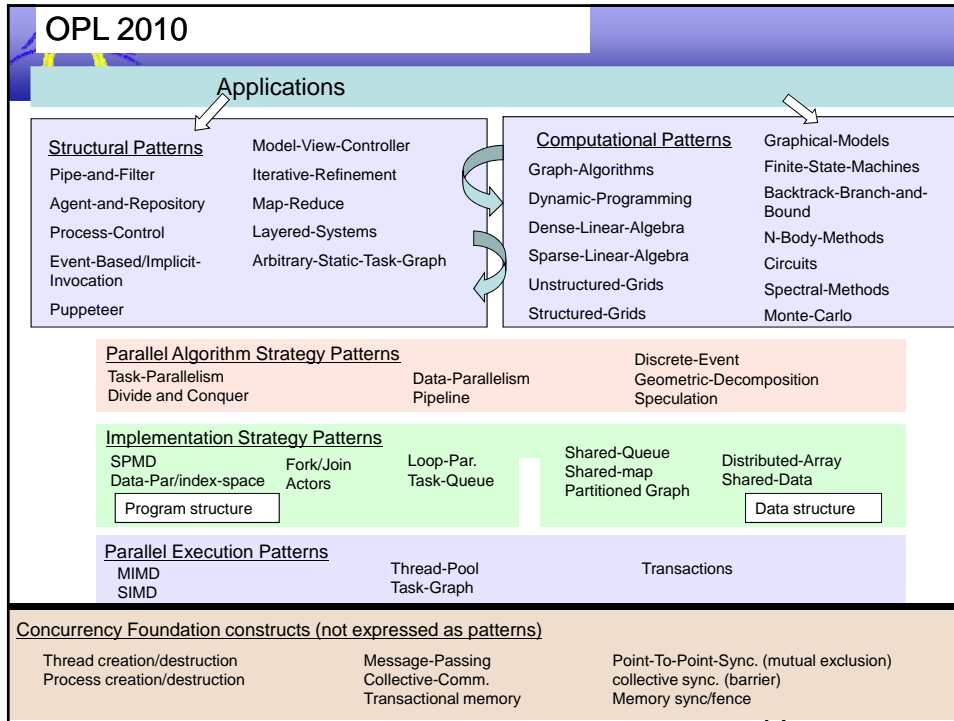
- Multicore/manycore design philosophy
 - **Multicore:** Devote significant transistor resources to single thread performance
 - **Manycore:** Maximizing computation throughput at the expense of single thread performance
- Architecture Trend:
 - Increasing vector unit width
 - Increasing numbers of cores per die
- Application Implications:
 - Must increase data access regularity
 - Must optimize synchronization cost

21/77

Outline

- Speech Recognition Application
- ➔ **Software Architecture using Patterns**
 - Identify Structural Patterns
 - Identify Computational Patterns
- Parallelization: (for each module)
 - Algorithm strategy pattern
 - Implementation strategy pattern
 - Execution patterns
- Conclusion

22/77



Intro

Inference Engine Architecture

- Recognition is a process of graph traversal
- Each time-step we need to identify the likely states in the recognition network given the observation acoustic signal
- From a the of active states we want to compute the next set of active states using probabilities of acoustic symbols and state transitions
- What **Structural pattern** is this?

Structural Patterns	Model-View-Controller
Pipe-and-Filter	Iterative-Refinement
Agent-and-Repository	Map-Reduce
Process-Control	Layered-Systems
Event-Based/Implicit-Invocation	Arbitrary-Static-Task-Graph
Puppeteer	

Viterbi Algorithm

25/77

Key computation: HMM Inference Algorithm

An instance of: **Graphical Models**

Implemented with: **Dynamic Programming**

- Finds the most-likely sequence of states that produced the

$$m[t][s_t] = \max_{s_{t-1}} m[t-1][s_{t-1}] \cdot P(s_t | s_{t-1}) \cdot P(x_t | s_t)$$

Viterbi Algorithm

Legends:

- S A State
- X An Observation
- $P(x_t | s_t)$
- $P(s_t | s_{t-1})$

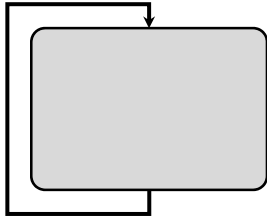
Markov Condition:

$$m[t][s_t] \doteq \max_{s_0, \dots, s_{t-1}} P(x_0, \dots, x_t, s_0, \dots, s_{t-1}, s_t)$$

J. Chong, Y. Yi, A. Faria, N.R. Satish and K. Keutzer, "Data-Parallel Large Vocabulary Continuous Speech Recognition on Graphics Processors", Emerging Applications and Manycore Arch. 2008, pp. 23-35, June 2008

26/77

Iterative Refinement Structural Pattern



- One iteration per time step
- Identify the set of probable states in the network given acoustic signal given current active state set
- Prune unlikely states
- Repeat

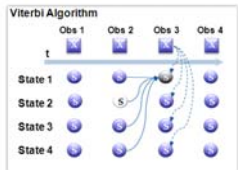
Structural Patterns	Model-View-Controller
Pipe-and-Filter	Iterative-Refinement
Agent-and-Repository	Map-Reduce
Process-Control	Layered-Systems
Event-Based/Implicit-Invocation	Arbitrary-Static-Task-Graph
Puppeteer	

27/77

Digging Deeper – Active Set Computation Architecture

- In each iteration we need to:
 - Compute observation probabilities of transitions from current states
 - Traverse the likely non-epsilon arcs to reach the set of next active states
 - Traverse the likely epsilon arcs to reach the set of next active states
- What **Structural pattern** is this?

Structural Patterns	Model-View-Controller
Pipe-and-Filter	Iterative-Refinement
Agent-and-Repository	Map-Reduce
Process-Control	Layered-Systems
Event-Based/Implicit-Invocation	Arbitrary-Static-Task-Graph
Puppeteer	



28/77

Digging Deeper – Active Set Computation Architecture

Phase 1 Observation probability computation

Phase 2 Graph-traversal

- In each iteration we need to:
 - Compute observation probabilities of transitions from current states
 - Traverse the likely non-epsilon arcs to reach the set of next active states
 - Traverse the likely epsilon arcs to reach the set of next active states
- What **Structural pattern** is this?

Viterbi Algorithm

Structural Patterns

Model-View-Controller
Iterative-Refinement
Map-Reduce
Layered-Systems
Arbitrary-Static-Task-Graph
Puppeteer

Pipe-and-Filter (highlighted)

Agent-and-Repository

Process-Control

Event-Based/Implicit-Invocation

29/77

Phase 1: Observation Probability computation Architecture

- Observation probabilities are computed from Gaussian Mixture Models
 - Each Gaussian probability in each mixture is independent
 - Probability for one phone state is the sum of all Gaussians times the mixture probability for that state
- What **Structural pattern** is this?

Gaussian Mixture Model for One Phone State

Mixture Components

Viterbi Algorithm

Structural Patterns

Model-View-Controller
Iterative-Refinement
Map-Reduce
Layered-Systems
Arbitrary-Static-Task-Graph
Puppeteer

Pipe-and-Filter (highlighted)

Agent-and-Repository

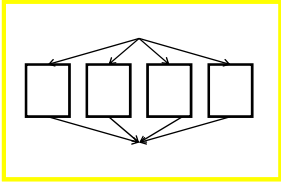
Process-Control

Event-Based/Implicit-Invocation

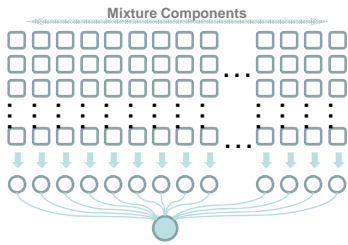
Dan Klein's CS288, Lecture 9

30/77

Map-Reduce Structural Pattern



Gaussian Mixture Model for One Phone State



- Map each mixture probability computation
- Reduce the result – accumulate the total probability for that state

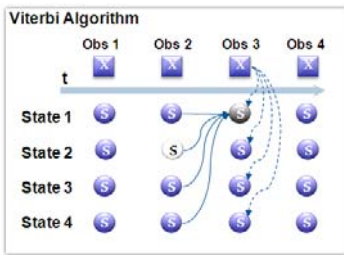
Structural Patterns	Model-View-Controller
Pipe-and-Filter	Iterative-Refinement
Agent-and-Repository	Map-Reduce
Process-Control	Layered-Systems
Event-Based/Implicit-Invocation	Arbitrary-Static-Task-Graph
Puppeteer	

31/77

Phase 2: Graph Traversal

- Now that we know the transition probabilities from current set of states, we need to compute the next set of active states (follow the likely transitions)
- Each transition is independent
- Multiple transitions might end in the same state
- The end result needs to be a set of most probable states from all transitions
- What **Structural pattern** is this? $m[t][s_t] = \max_{s_{t-1}} m[t-1][s_{t-1}] \cdot P(s_t|s_{t-1}) \cdot P(x_t|s_t)$

Structural Patterns	Model-View-Controller
Pipe-and-Filter	Iterative-Refinement
Agent-and-Repository	Map-Reduce
Process-Control	Layered-Systems
Event-Based/Implicit-Invocation	Arbitrary-Static-Task-Graph
Puppeteer	



32/77

Map-Reduce Structural Pattern- again

- Map each mixture probability computation
- Reduce the result – accumulate the total probability for that state

$$m[t][s_t] = \max_{s_{t-1}} m[t-1][s_{t-1}] \cdot P(s_t | s_{t-1}) \cdot P(x_t | s_t)$$

Viterbi Algorithm

	Obs 1	Obs 2	Obs 3	Obs 4
t	X	X	X	X
State 1	S	S	S	S
State 2	S	S	S	S
State 3	S	S	S	S
State 4	S	S	S	S

Structural Patterns

Model-View-Controller
Iterative-Refinement
Map-Reduce
Layered-Systems
Arbitrary-Static-Task-Graph
Puppeteer

33/77

High Level Structure of Engine

Inference Engine

- Active Set Computation
- Phase 1: Observation Probability Computation
- Phase 2: Graph Traversal

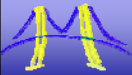
Structural Patterns

Pipe-and-Filter
Agent-and-Repository
Process-Control
Event-Based/Implicit-Invocation
Puppeteer

Structural Patterns

Model-View-Controller
Iterative-Refinement
Map-Reduce
Layered-Systems
Arbitrary-Static-Task-Graph

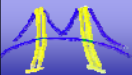
33/77



Outline

- Speech Recognition Application
- Software Architecture using Patterns
 - Identify Structural Patterns
 - **Identify Computational Patterns**
- Parallelization: (for each module)
 - Algorithm strategy pattern
 - Implementation strategy pattern
 - Execution patterns
- Conclusion

35/77

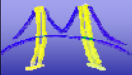


What about Computation?

- Active Set Computation:
 - Phase 1: Compute observation probability of transitions given current set of states
 - Phase 2: Traverse arcs to determine next set of most likely active states
- What **Computational Patterns** are these?

Computational Patterns	Graphical-Models
Graph-Algorithms	Finite-State-Machines
Dynamic-Programming	Backtrack-Branch-and-Bound
Dense-Linear-Algebra	N-Body-Methods
Sparse-Linear-Algebra	Circuits
Unstructured-Grids	Spectral-Methods
Structured-Grids	Monte-Carlo

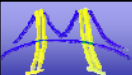
36/77



Outline


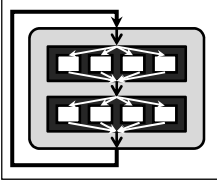
- Speech Recognition Application
- Software Architecture using Patterns
 - Identify Structural Patterns
 - Identify Computational Patterns
- ➔ **Parallelization: (for each module)**
 - Algorithm strategy pattern
 - Implementation strategy pattern
 - Execution patterns
- Conclusion

37/77



Now to Parallelism – Inference Engine

- Structural Patterns: Iterative Refinement
- Computational Patterns: Dynamic Programming
- Inference engine and Active Set computation is sequential
 - Let's look at Phase 1 and Phase 2
- What Parallel **Algorithm Strategy** can we use?

Parallel Algorithm Strategy Patterns		
Task-Parallelism	Data-Parallelism	Discrete-Event
Divide and Conquer	Pipeline	Geometric-Decomposition
		Speculation

38/77

Now to Parallelism – Inference Engine

- Phase 1: Observation Probability Computation
 - Structural: MapReduce
 - Computational: Graphical Models
- Compute cluster Gaussian Mixture Probabilities for each transition label
- Hint:
 - Look at data dependencies (or lack there-of)

Viterbi Algorithm

Parallel Algorithm Strategy Patterns

Task-Parallelism Divide and Conquer	Data-Parallelism Pipeline	Discrete-Event Geometric-Decomposition Speculation
--	------------------------------	--

39/77

Now to Parallelism – Inference Engine

- Phase 1: Observation Probability Computation
 - Structural: MapReduce
 - Computational: Graphical Models
- Compute cluster Gaussian Mixture Probabilities for each transition label
- Map reduce necessarily implies data-parallelism

Viterbi Algorithm

Parallel Algorithm Strategy Patterns

Task-Parallelism Divide and Conquer	Data-Parallelism Pipeline	Discrete-Event Geometric-Decomposition Speculation
--	------------------------------	--

40/77

Observation Probability Pattern Computation

<p>Structural Patterns</p> <ul style="list-style-type: none"> Pipe-and-Filter Agent-and-Repository Process-Control Event-Based/Implicit-Invocation Puppeteer 	<p>Model-View-Controller</p> <p>Iterative-Refinement</p> <p>Map-Reduce</p> <p>Layered-Systems</p> <p>Arbitrary-Static-Task-Graph</p>
--	---

<p>Parallel Algorithm Strategy Patterns</p> <ul style="list-style-type: none"> Task-Parallelism Divide and Conquer 	<p>Computational Patterns</p> <ul style="list-style-type: none"> Graph-Algorithms Dynamic-Programming Dense-Linear-Algebra Sparse-Linear-Algebra Unstructured-Grids Structured-Grids
---	---

<p>Implementation Strategy Patterns</p> <ul style="list-style-type: none"> SPMD Data-Par/index-space Program structure 	<p>Fork/Join Actors</p> <p>Loop-Par. Task-Queue</p> <p>Shared-Queue</p> <p>Shared-map</p> <p>Partitioned Graph</p> <p>Data structure</p>
--	--

<p>Parallel Execution Patterns</p> <ul style="list-style-type: none"> MIMD SIMD 	<p>Thread-Pool Task-Graph</p> <p>Transactions</p>
--	---

Implementation strategy: Data structure?

41/77

Observation Probability Pattern

<p>Structural Patterns</p> <ul style="list-style-type: none"> Pipe-and-Filter Agent-and-Repository Process-Control Event-Based/Implicit-Invocation Puppeteer 	<p>Model-View-Controller</p> <p>Iterative-Refinement</p> <p>Map-Reduce</p> <p>Layered-Systems</p> <p>Arbitrary-Static-Task-Graph</p>
--	---

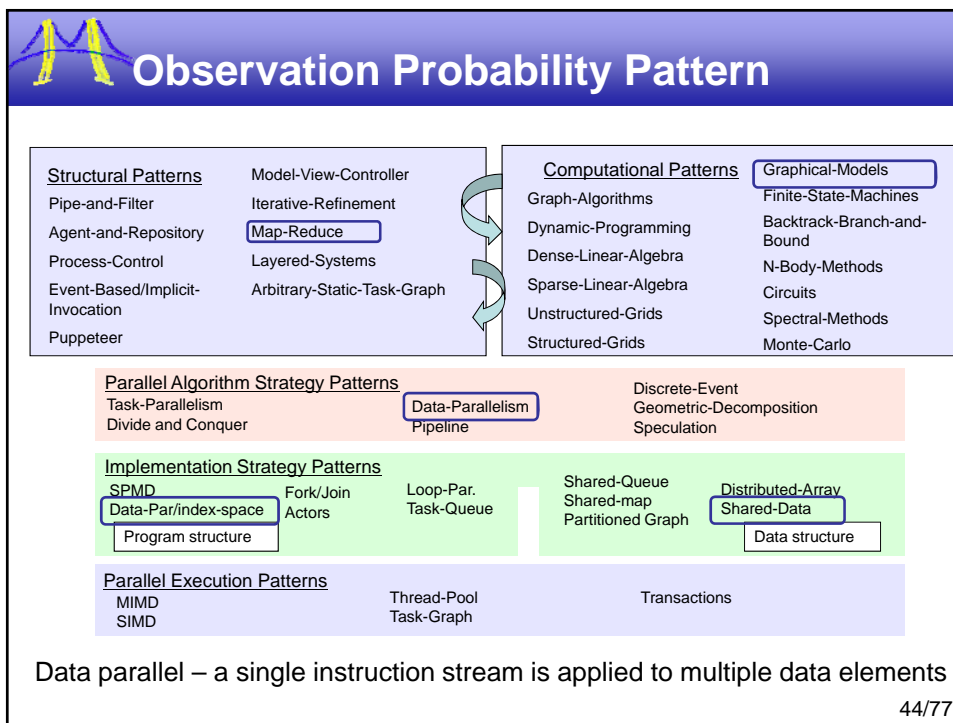
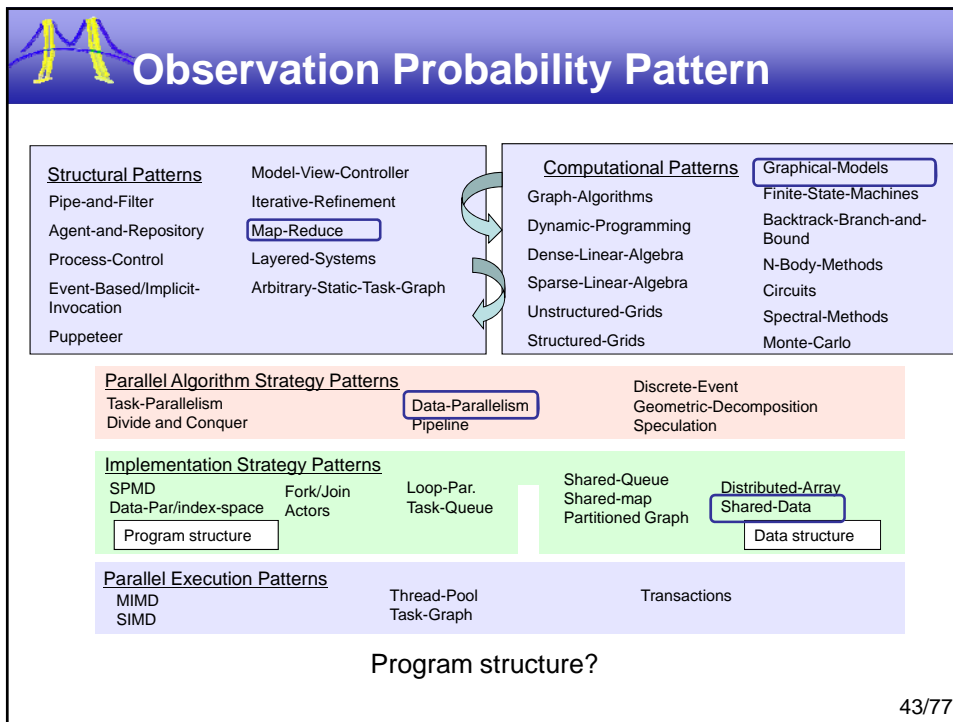
<p>Parallel Algorithm Strategy Patterns</p> <ul style="list-style-type: none"> Task-Parallelism Divide and Conquer 	<p>Computational Patterns</p> <ul style="list-style-type: none"> Graph-Algorithms Dynamic-Programming Dense-Linear-Algebra Sparse-Linear-Algebra Unstructured-Grids Structured-Grids
---	---

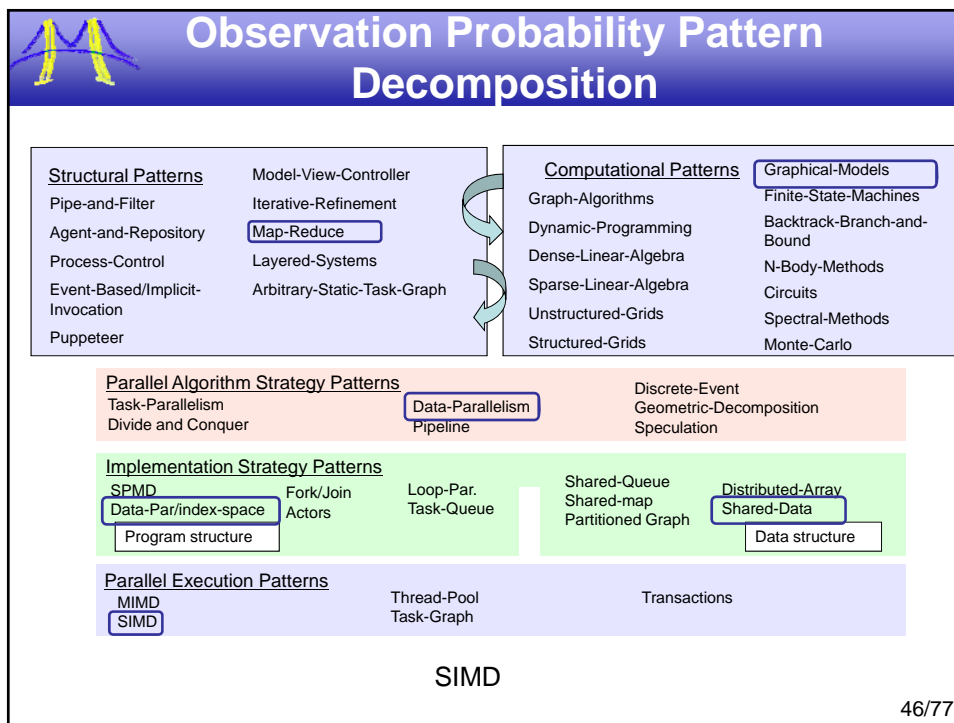
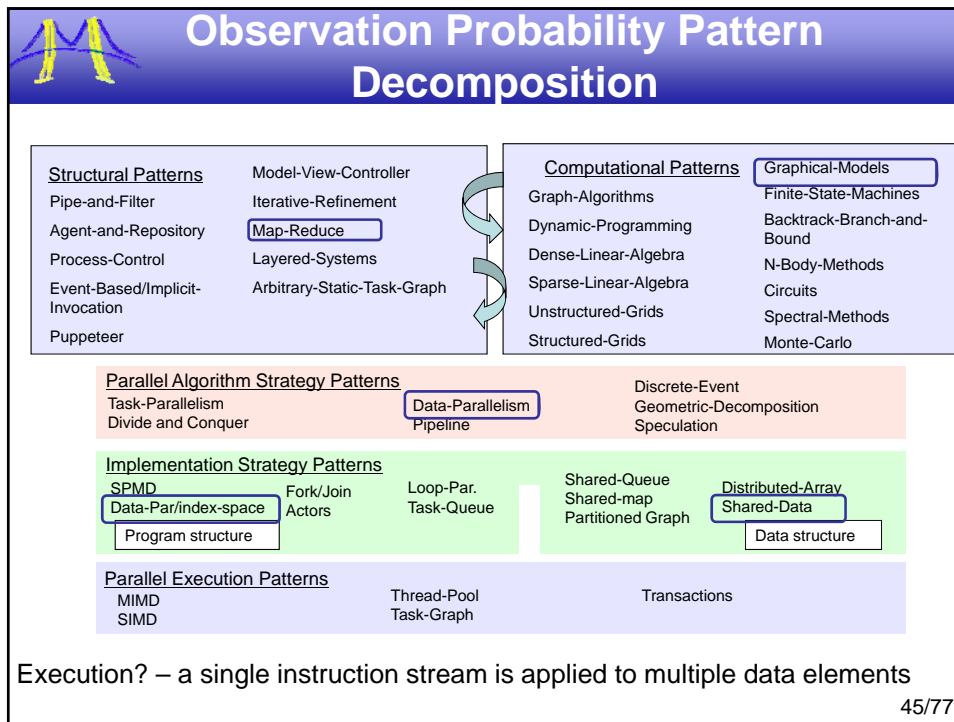
<p>Implementation Strategy Patterns</p> <ul style="list-style-type: none"> SPMD Data-Par/index-space Program structure 	<p>Fork/Join Actors</p> <p>Loop-Par. Task-Queue</p> <p>Shared-Queue</p> <p>Shared-map</p> <p>Partitioned Graph</p> <p>Distributed-Array Shared-Data</p> <p>Data structure</p>
--	---

<p>Parallel Execution Patterns</p> <ul style="list-style-type: none"> MIMD SIMD 	<p>Thread-Pool Task-Graph</p> <p>Transactions</p>
--	---

Gaussian Mixture Model is shared among all computations – read only

42/77





Now to Parallelism Pt2 – Inference Engine

- Phase 2: Graph Traversal
 - Structural: MapReduce
 - Computational: Graph algorithms/graph traversal
- The recognition network is a finite state transducer, represented as a weighted and labeled graph
- Decoding on this graph is Breadth-First Traversal
- What **Parallel Algorithmic Strategy** can we use?

Viterbi Algorithm

- Hint:
 - What are the operands?
 - What are the dependences?

Parallel Algorithm Strategy Patterns

Task-Parallelism
Divide and Conquer

Data-Parallelism
Pipeline

Discrete-Event
Geometric-Decomposition
Speculation

47/77

Now to Parallelism – Inference Engine

- Phase 2: Graph Traversal
 - Structural: MapReduce
 - Computational: Graph Traversal
- The recognition network is a finite state transducer, represented as a weighted and labeled graph
- Decoding on this graph is Breadth-First Traversal

Viterbi Algorithm

Data Parallelism!
Each next state computation can be computed independently.

Parallel Algorithm Strategy Patterns

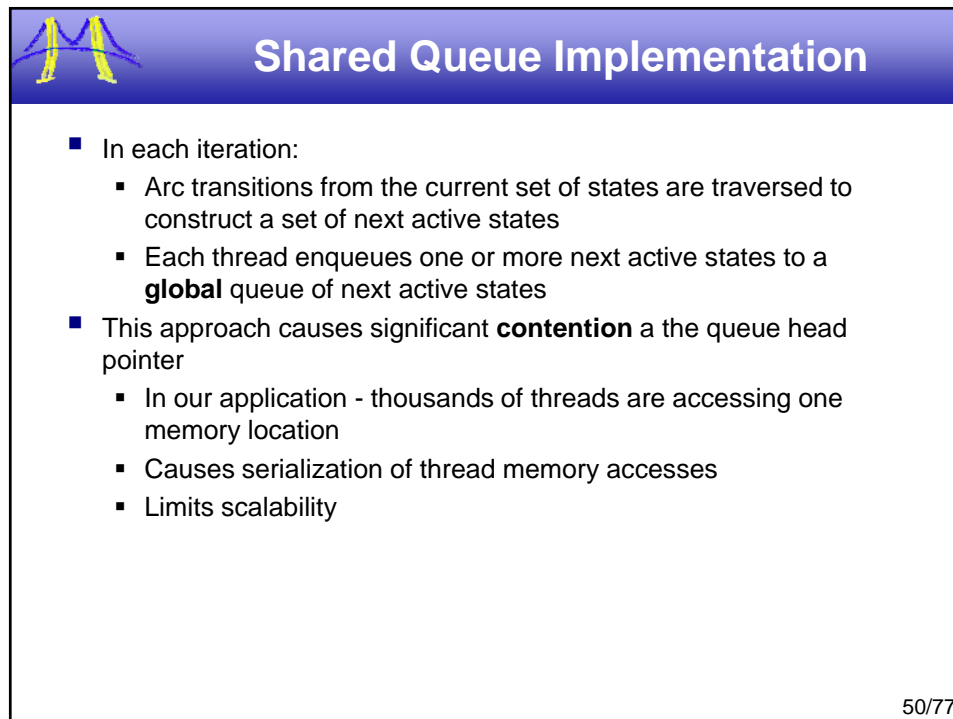
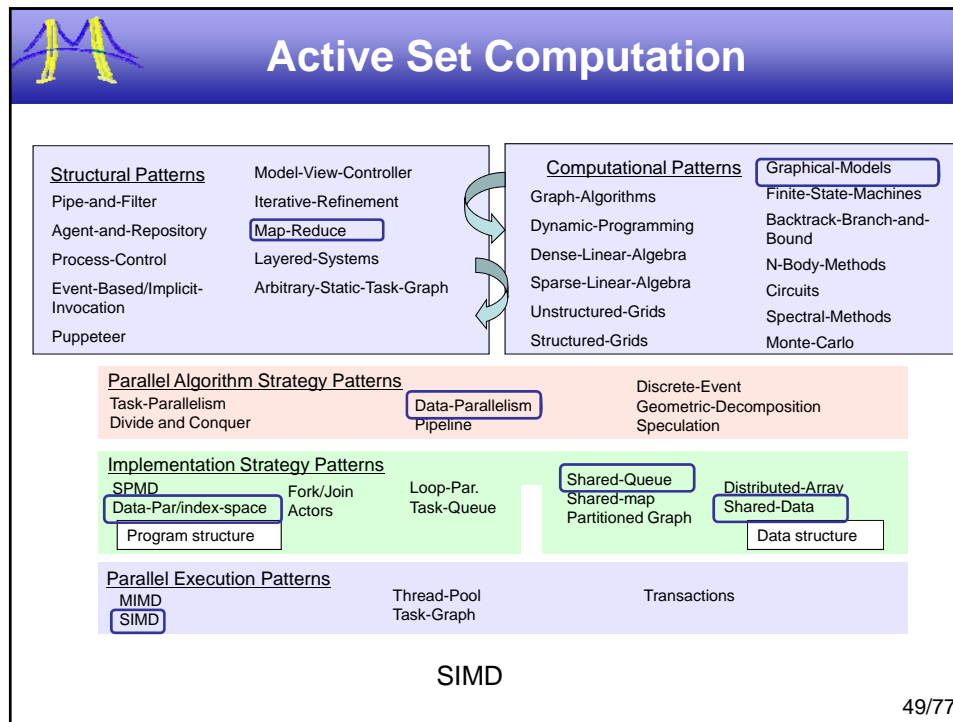
Task-Parallelism
Divide and Conquer

Data-Parallelism

Pipeline

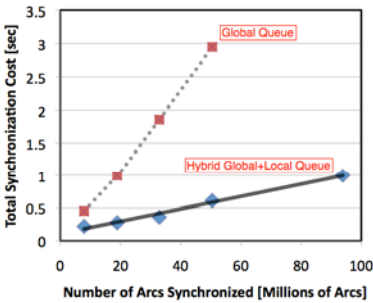
Discrete-Event
Geometric-Decomposition
Speculation

48/77



Shared Queue Implementation

- Solution to the queue head pointer contention -> distributed queue
 1. Each thread in a thread block writes to a local queue of next active states
 2. Local queues are merged into a global queue



- Contention on global queue pointer is reduced from #threads to #blocks
- Significantly improves scalability

51/77

Speech Reference Implementation

Manycore GPU			CPU		
Data	Control	Data	Control	Data	Backtrack Table
Active Set			Read Files		
	LM	HMM	Initialize data structures		
	W	W			
	W	R			
	R	R			
	W				
	R	R			
	W				
	R		Collect Backtrack Info		W
			Backtrack		R
			Output Results		W
					R

Jike Chong, Ekaterina Gonina, Youngmin Yi, Kurt Keutzer, "A Fully Data Parallel WFST-based Large Vocabulary Continuous Speech Recognition on a Graphics Processing Unit", Proceeding of the 10th Annual Conference of the International Speech Communication Association (InterSpeech), page 1183 – 1186, September, 2009.

Phase 0

Iteration Control

Prepare ActiveSet

Phase 1

Compute Observation Probability

Phase 2

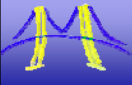
For each active arc:
• Compute arc transition probability

Copy results back to CPU

Kisun You, Jike Chong, Youngmin Yi, Ekaterina Gonina, Christopher Hughes, Yen-Kuang Chen, Wonyong Sung, Kurt Keutzer, "Parallel Scalability in Speech Recognition: Inference engine in large vocabulary continuous speech recognition", IEEE Signal Processing Magazine, vol. 26, no. 6, pp. 124-135, November 2009.

Jike Chong, Ekaterina Gonina, Kisun You, Kurt Keutzer, "Scalable Parallelization of Automatic Speech Recognition", Invited book chapter in Scaling Up Machine Learning, an upcoming 2010 Cambridge University Press book.

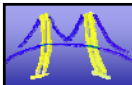
52/77



Summary

- A good architect needs to understand:
 - Structural patterns
 - Computational patterns
 - Refinement through Our Pattern Language
- Graph algorithms and graphical models are critical to many applications
- Graph algorithms are especially difficult to parallelize and library support is inadequate
- There will be at least a decade of hand-crafted solutions
- We achieved good results on parallelizing large-vocabulary automatic speech recognition

53/77



Extras

54/77

Example: Breadth First Search

```

1 template<class IncidenceGraph, class Buffer, class BFSVisitor, class ColorMap>
2 void
3 breadth_first_search (const IncidenceGraph& g,
4                       typename graph_traits<VertexListGraph>::vertex_descriptor s,
5                       Buffer& Q, BFSVisitor vis, ColorMap color)
6 {
7     put(color, s, Color::gray());          vis.discover_vertex (s, g);
8     Q.push(s);
9     while (! Q.empty()) {
10        Vertex u = Q.top(); Q.pop();       vis.examine_vertex(u, g);
11        for (tie (ei, ei_end) = out_edges(u, g); ei != ei_end; ++ei) {
12            Vertex v = target(*ei, g);    vis.examine_edge(*ei, g);
13            ColorValue v_color = get(color, v);
14            if (v_color == Color::white()) {
15                put(color, v, Color::gray());
16                Q.push(v);
17            } else {
18                if (v_color == Color::gray())
19                    vis.tree_edge (*ei, g);
20                else
21                    vis.non_tree_edge (*ei, g);
22                put(color, u, Color::black());
23            } // end while
24        } // end for
25    }
26 }

```

Q.push(s);

Vertex u = Q.top(); Q.pop();

ColorValue v_color = get(color, v);

if (v_color == Color::white()) {

put(color, v, Color::gray());

Q.push(v);

vis.discover_vertex (s, g);

vis.examine_vertex(u, g);

vis.examine_edge(*ei, g);

vis.tree_edge (*ei, g);

vis.discover_vertex (v, g);

vis.non_tree_edge (*ei, g);

vis.gray_target (*ei, g);

vis.black_target (*ei, g);

Breadth first search

- Distributed Graph
- Distributed Queues
- Distributed Visitors
- Distributed Property Map

Algorithm
Visitors

55/77

Example: Distributed BFS

❖ Distributed Graph

```

typedef adjacency_list<
    /* edge list = */ listS,
    /* vertex list = */ vecS,
    /* directedness = */ bidirectionalS,
    property<vertex_distance_t, double>,
    property<edge_weight_t, double>> Digraph;

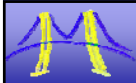
typedef adjacency_list<
    /* edge list = */ listS,
    /* vertex list = */
    distributedS<mpi::bsp_process_group, vecS>,
    /* directedness = */ bidirectionalS,
    property<vertex_distance_t, double>,
    property<edge_weight_t, double>>
    DistributedDigraph;

```

(a) Distributed Graph

(b) Distributed adjacency list representation

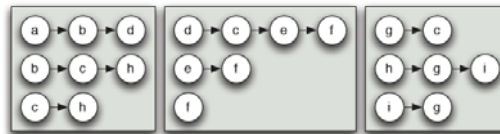
56/77



Example: Distributed BFS

❖ Distributed Queues

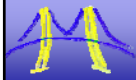
- pop() from local queues
- push() sends message to the vertex owner
- empty() exhaust local queue and synchronize with other processors to determine termination condition
- Messages are only received after all processors have completed operation at one level



(b) Distributed adjacency list representation

57

57/77



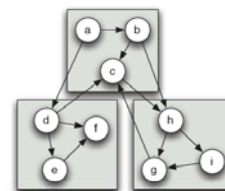
Example: Distributed BFS

❖ Distributed Visitors

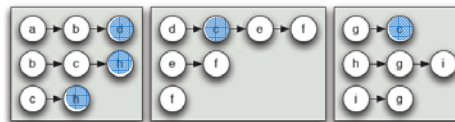
- Owner-compute scheme, so distributed version is the same as sequential visitor

❖ Distributed Property Map

- Local Property Map
 - Store local properties for local vertices and edges
- Ghost Cells
 - Store properties for ghost cells
- Process Group
 - Communication medium
- Data Race Resolver
 - Decides among various put() messages sent to the Distributed Property Map



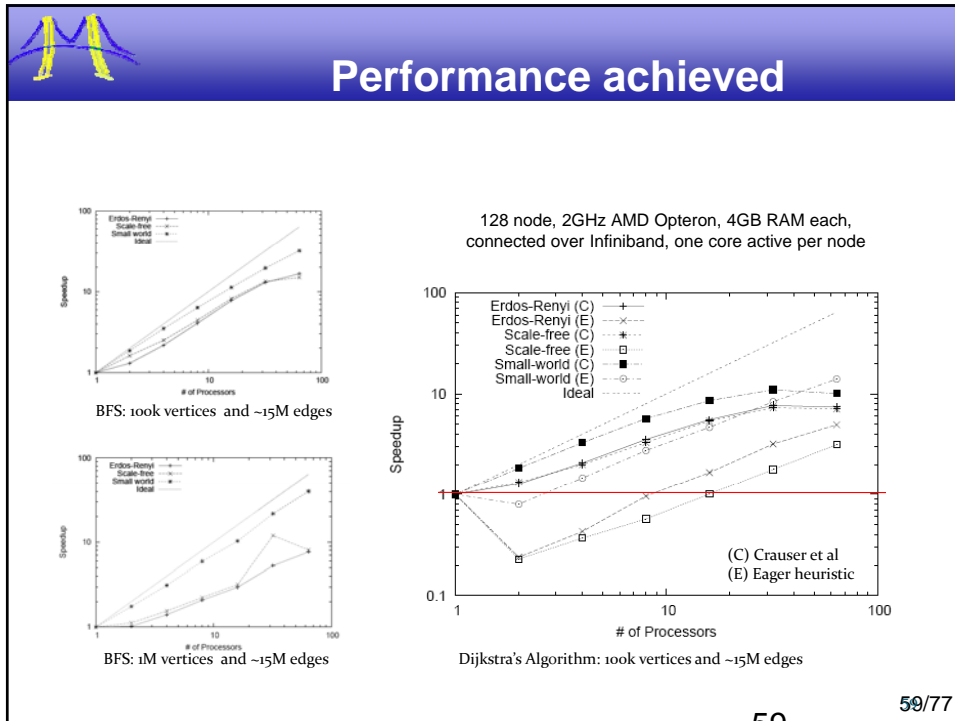
(a) Distributed Graph



(b) Distributed adjacency list representation

58

58/77



Discussion

- ❖ Graph traversal algorithm characteristic:
 1. Input data-driven computation
 2. Unstructured problems
 3. Poor data locality
 4. High data access to computation ratio
- ❖ High demand for low memory latency and poor data locality makes it challenging for PEs without fine-grain multiprocessing
- ❖ Pointer chasing mainly involves integer operations
 - Niagara type platforms seems suitable for this application domain
 - What about GPGPU?
- ❖ What how well would our scheduling algorithms map to Parallel BGL?

60/77