CS 267: Applications of Parallel Computers

Dynamic Load Balancing

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Sources of inefficiency in parallel codes

- Poor single processor performance
 - Typically in the memory system (recall matmul homework)
- Too much parallelism overhead
 - · Thread creation, synchronization, communication
- Load imbalance
 - · Different amounts of work across processors
 - · Computation and communication
 - · Different speeds (or available resources) for the processors
 - · Possibly due to load on shared machine
 - · Heterogeneous resources (eg CPU + GPU)
- How to recognize load imbalance
 - Time spent at synchronization is high and is uneven across processors, but not always so simple ...

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Outline

- · Motivation for Load Balancing
- · Recall graph partitioning as static load balancing technique
- · Overview of load balancing problems, as determined by
 - Task costs
 - · Task dependencies
 - · Locality needs
- · Spectrum of solutions
 - · Static all information available before starting
 - · Semi-Static some info before starting
 - · Dynamic little or no info before starting
 - · Or: how rapidly do costs/dependencies/locality needs change?
- · Survey of solutions
 - · How each one works
 - · Theoretical bounds, if any
 - · When to use it, tools

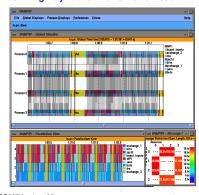
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Measuring Load Imbalance

- · Challenges:
 - · Can be hard to separate from high synchronization overhead
 - Especially subtle if not bulk-synchronous
 - "Spin locks" can make synchronization look like useful work
 - Note that imbalance may change over phases
 - Insufficient parallelism always leads to load imbalance
 - Tools like IPM,TAU can help (acts.nersc.gov)



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Review of Graph Partitioning - static case

- · Partition G(N,E) so that
 - $N = N_1 U ... U N_p$, with each $IN_i I \sim INI/p$
 - · As few edges connecting different Ni and Nk as possible
- If N = {tasks}, each unit cost, edge e=(i,j) means task i has to communicate with task j, then partitioning means
 - balancing the load, i.e. each INiI ~ INI/p
 - · minimizing communication volume
- Optimal graph partitioning is NP complete, so we use heuristics (see earlier lectures)
 - · Spectral, Kernighan-Lin, Multilevel ...
- · Good software available
 - · (Par)METIS, Scotch, Zoltan, ...
- · Speed of partitioner trades off with quality of partition
 - · Better load balance costs more; may or may not be worth it
- Need to know tasks, communication pattern before starting
 - · What if you don't? Can redo partitioning, but not frequently

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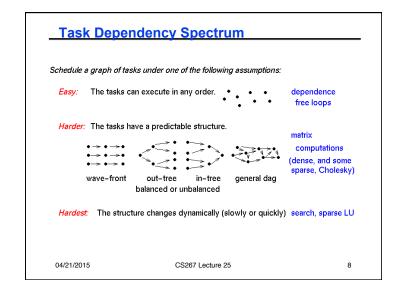
Load Balancing Overview

Load balancing differs with properties of the tasks

- · Tasks costs
 - · Do all tasks have equal costs?
 - · If not, when are the costs known?
 - · Before starting, when task created, or only when task ends
- · Task dependencies
 - · Can all tasks be run in any order (including parallel)?
 - · If not, when are the dependencies known?
 - · Before starting, when task created, or only when task ends
 - · One task may prematurely end another task (eg search)
- Locality (may tradeoff with load balance)
 - Is it important for some tasks to be scheduled on the same processor (or nearby) to reduce communication cost?
 - When is the information about communication known?
- · If properties known only when tasks end
 - · Are statistics fixed, change slowly, change abruptly?

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Task Cost Spectrum Schedule a set of tasks under one of the following assumptions: Easy: The tasks all have equal (unit) cost. branch-free loops Harder: The tasks have different, but known, times. p bins sparse matrix—vector multiply Hardest: The task costs unknown until after execution. GCM, circuits, search



Task Locality Spectrum (Communication)

Schedule a set of tasks under one of the following assumptions:

Easy: The tasks, once created, do not communicate.

embarrassingly parallel

Harder: The tasks communicate in a predictable pattern.

regular



PDE solver

Hardest: The communication pattern is unpredictable.

discrete event simulation

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Spectrum of Solutions

A key question is when certain information about the load balancing problem is known.

Leads to a spectrum of solutions:

- Static scheduling. All information is available to scheduling algorithm, which runs before any real computation starts.
 - · Off-line algorithms, eg graph partitioning, DAG scheduling
 - · Still might use dynamic approach if too much information
- Semi-static scheduling. Information may be known at program startup, or the beginning of each timestep, or at other well-defined points.
 Offline algorithms may be used even though the problem is dynamic.
 - · eg Kernighan-Lin, as in Zoltan
- · Dynamic scheduling. Information is not known until mid-execution.
 - · On-line algorithms main topic today

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Dynamic Load Balancing

- Motivation for dynamic load balancing
 - · Search algorithms as driving example
- Centralized load balancing
 - Overview
 - · Special case for schedule independent loop iterations
 - · Makes most sense in shared memory environment
 - · Hard to scale to large numbers of processors
- Distributed load balancing
 - · Overview randomization often used
 - Engineering
 - · Theoretical results

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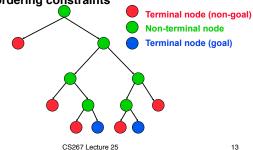
Search

- · Search problems are often:
 - · Computationally expensive
 - Have very different parallelization strategies than physical simulations.
 - Require dynamic load balancing
- · Examples:
 - · Optimal layout of VLSI chips
 - · Robot motion planning
 - · Chess and other games (N-queens)
 - · Speech processing
 - · Constructing phylogeny tree from set of genes

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Example Problem: Tree Search

- · In Tree Search the tree unfolds dynamically
- May be a graph if there are common sub-problems along different paths
- Graphs unlike meshes which are precomputed and have no ordering constraints



Sequential Search Algorithms

Depth-first search (DFS)

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- · Simple backtracking
 - · Search to bottom, backing up to last choice if necessary
- · Depth-first branch-and-bound
 - Keep track of best solution so far ("bound")
 - · Cut off sub-trees that are guaranteed to be worse than bound
- · Iterative Deepening ("in between" DFS and BFS)
 - · Choose a bound d on search depth, and use DFS up to depth d
 - · If no solution is found, increase d and start again
 - · Can use an estimate of cost-to-solution to get bound on d
- Breadth-first search (BFS)
 - Search all nodes at distance 1 from the root, then distance 2, and so on

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Depth vs Breadth First Search (Review)

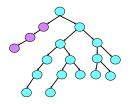
- · DFS with Explicit Stack little parallelism
 - · Put root into Stack
 - · Stack is data structure where items added to and removed from the top only
 - · While Stack not empty
 - · If node on top of Stack satisfies goal of search, return result, else
 - Mark node on top of Stack as "searched"
 - If top of Stack has an unsearched child, put child on top of Stack, else remove top of Stack
- BFS with Explicit Queue lots of parallelism (depending on graph)
 - · Put root into Queue
 - · Queue is data structure where items added to end, removed from front
 - · While Queue not empty
 - · If node at front of Queue satisfies goal of search, return result, else
 - Mark node at front of Queue as "searched"
 - If node at front of Queue has any unsearched children, put them all at end of Queue
 - Remove node at front from Queue

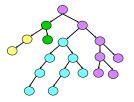
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Parallel Search

- · Consider simple backtracking search
- Try static load balancing: spawn each new task on an idle processor, until all have a subtree





Load balance on 2 processors

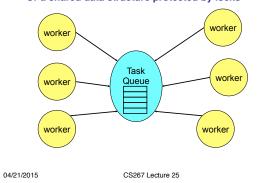
Load balance on 4 processors

· We can and should do better than this ...

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Centralized Scheduling

- · Keep a queue of task waiting to be done
 - · May be done by manager task
 - · Or a shared data structure protected by locks



Centralized Task Queue: Scheduling Loops

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- · When applied to loops, often called self scheduling
 - · Assume independent loop iterations, varying run times
- Typically, don't want to grab smallest unit of parallel work, i.e., a single loop iteration
 - · Too much contention at shared queue
- Instead, choose a chunk of tasks of size K.
 - · If K is large, access overhead for task queue is small
 - If K is small, we are likely to have even finish times (load balance)
- (at least) Four Variations:
 - 1. Use a fixed chunk size
 - 2. Guided self-scheduling
 - 3. Tapering
- 4. Weighted Factoring

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Centralized Task Queue: Scheduling Loops

- · When applied to loops, often called self scheduling:
 - · Tasks may be range of loop indices to compute
 - · Assumes independent iterations
 - Loop body has unpredictable time (branches) or the problem is not interesting
- Originally designed for:
 - Scheduling loops by compiler (or runtime-system)
 - Original paper by Tang and Yew, ICPP 1986
- Properties
 - · Dynamic, online scheduling algorithm
 - · Good for a small number of processors (centralized)
 - · Special case of task graph independent tasks, known at once

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Variation 1/4: Fixed Chunk Size

- Kruskal and Weiss give a technique for computing the optimal chunk size (IEEE Trans. Software Eng., 1985)
- Requires a lot of information about the problem characteristics
 - · e.g., task costs, number of tasks, cost of scheduling
 - Probability distribution of runtime of each task (same for all)
 - · Assumes distribution is IFR = "Increasing Failure Rate"
 - For any t>0, P(X > x+t | X > x) is a decreasing function of x
 - $K_{opt} = (2^{\frac{1}{2}} * \# tasks * time_to_access_queue/(\sigma * p * (log p)^{\frac{1}{2}}))^{\frac{2}{3}}$
- · Not very useful in practice
 - · Distribution must be known at loop startup time

Variation 2/4: Guided Self-Scheduling

- Idea: use larger chunks at the beginning to avoid excessive overhead and smaller chunks near the end to even out the finish times.
 - The chunk size K_i at the i^{th} access to the task pool is given by $K_i = ceiling(R/p)$
 - · where R_i is the total number of tasks remaining and
 - · p is the number of processors
- See Polychronopoulos & Kuck, "Guided Self-Scheduling: A Practical Scheduling Scheme for Parallel Supercomputers," IEEE Transactions on Computers, Dec. 1987.

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Variation 4/4: Weighted Factoring

- Idea: similar to self-scheduling, but divide task cost by computational power of requesting node
- · Useful for heterogeneous systems
- Also useful for shared resource clusters, e.g., built using all the machines in a building
 - as with Tapering, historical information is used to predict future speed
 - "speed" may depend on the other loads currently on a given processor
- See Hummel, Schmit, Uma, and Wein, SPAA '96
 - · includes experimental data and analysis

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Variation 3/4: Tapering

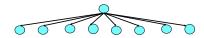
- Idea: the chunk size, K_i is a function of not only the remaining work, but also the task cost variance
 - · variance is estimated using history information
 - high variance => small chunk size should be used
 - low variance => larger chunks OK
- See S. Lucco, "Adaptive Parallel Programs," PhD Thesis, UCB, CSD-95-864, 1994.
 - · Gives analysis (based on workload distribution)
 - Also gives experimental results -- tapering always works at least as well as GSS, although difference is often small

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Summary: When is Self-Scheduling a Good Idea?

Useful when:

- · A batch (or set) of tasks without dependencies
 - can also be used with dependencies, but most analysis has only been done for task sets without dependencies



- The cost of each task is unknown
- Locality is not important
- Shared memory machine, or at least number of processors is small – centralization is OK

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Cilk: A Language with Built-in Load balancing

A C language for programming dynamic multithreaded applications on shared-memory multiprocessors.

CILK (Leiserson et al) (supertech.lcs.mit.edu/cilk)

- Created startup company called CilkArts
- Acquired by Intel

Example applications:

- virus shell assembly
- graphics rendering
- *n*-body simulation
- heuristic search

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- dense and sparse matrix computations
- friction-stir welding simulation
- artificial evolution

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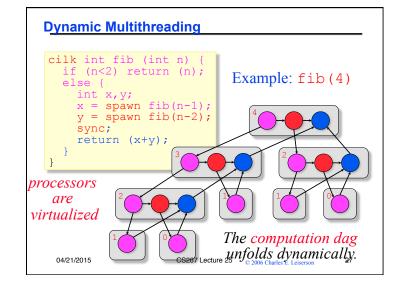
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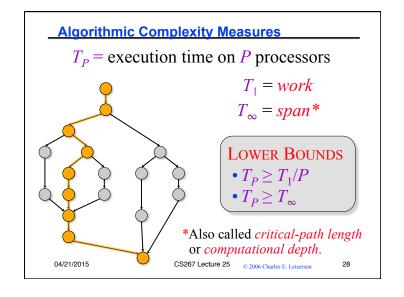
Fibonacci Example: Creating Parallelism

```
int fib (int n) {
if (n<2) return (n);
                            Cilk code
  else {
    int x, y;
                     cilk int fib (int n) {
    x = fib(n-1);
                       if (n<2) return (n);
    y = fib(n-2);
                        else {
    return (x+y);
                          int x, y;
                          x = spawn fib(n-1);
                          y = spawn fib(n-2);
                          sync;
     C elision
                          return (x+y);
```

Cilk is a *faithful* extension of C. A Cilk program's *serial elision* is always a legal implementation of Cilk semantics. Cilk provides *no* new data types.

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Speedup

Definition: $T_1/T_P = speedup$ on P processors.

If $T_1/T_P = \Theta(P) \leq P$, we have *linear speedup*;

= P, we have *perfect linear speedup*; > P, we have superlinear speedup,

which is not possible in our model, because of the lower bound $T_P \ge T_1/P$.

 $\overline{T_1/T_{\infty}} = available parallelism$

=the average amount of work per step along the span (critical path).

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Greedy Scheduling

IDEA: Do as much as possible on every step.

Definition: A thread is *ready* if all its predecessors have executed.

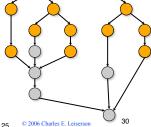
Complete step

- $\geq P$ threads ready.
- Run any *P*.

Incomplete step

- < *P* threads readv.
- Run all of them.

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P = 3

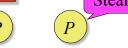
Cilk's Work-Stealing Scheduler

Each processor maintains a *work deque* of ready threads, and it manipulates the bottom of the deque like a stack.











When a processor runs out of work, it steals a thread from the top of a random victim's deque.

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Performance of Work-Stealing

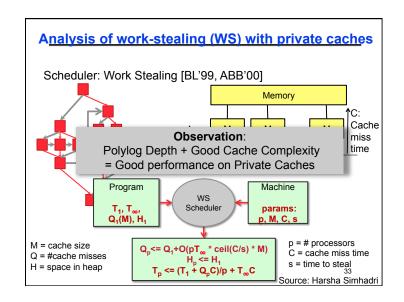
Theorem: Cilk's work-stealing scheduler achieves an expected running time of

$$T_p \le T_1/P + O(T_\infty)$$

on *P* processors.

Pseudoproof. A processor is either working or stealing. The total time all processors spend working is T_1 . Each steal has a 1/P chance of reducing the span by 1. Thus, the expected cost of all steals is $O(PT_{\infty})$. Since there are P processors, the expected time is

$$(T_1 + O(PT_\infty))/P = T_1/P + O(T_\infty) . \blacksquare$$
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Further analyses of Cilk's Performance

- Bounds on #cache misses caused by work stealing if each processor has private cache, single shared (slow) memory
- · Bounds extended to hierarchical memories
- Space needed (for stacks) by P processors at most P times space needed by one processor
- · General conclusions:
 - Work stealing good idea if execution DAG not too deep, and sequential implementation would not generate too many cache misses

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Extensions/variations on work stealing

- Parallel-Depth First Schedule
 - · Assume Depth First order of tasks known, prioritize in this order
 - Greedy work schedule where "ready tasks" executed in priority order
 - · Better bounds on parallel space, locality on shared caches
- Space Bounded schedulers
 - · Anchor tasks to preserve locality
 - · Do not allow tasks to move, once assigned
 - · Assignments must not allow caches to overflow

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Space Bounds **Theorem.** Let S_1 be the stack space required by a serial execution of a Cilk program. Then, the space required by a *P*-processor execution is at most $S_P = PS_1$. P=3*Proof* (by induction). The work-stealing algorithm maintains the busy-leaves property: every extant procedure frame with no extant descendents has a processor working on it. 04/21/2015 CS267 Lecture 25 © 2006 Charles E. Leiserso

DAG Scheduling software

- QUARK (U. Tennessee)
 - Library developed to support PLASMA for pipelining ("synchronization avoiding") dense linear algebra
- SMPss (Barcelona)
 - Compiler based; Data usage expressed via pragmas; Proposal to be in OpenMP; Recently added GPU support
- StarPU (INRIA)
 - Library based; GPU support; Distributed data management; Codelets=tasks (map CPU, GPU versions)
- DAGUE/DPLASMA (MPI group work)
 - Needs a compact DAG representation; Distributed memory; Designed to be very, very scalable
- Other tools (e.g., fork-join graphs only)
 - Cilk, Intel Threaded Building Blocks (TBB); Microsoft CCR, \dots_{37}

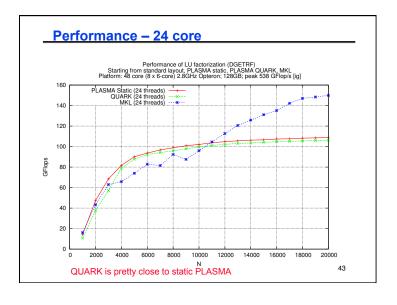
Pipelining: Cholesky Inversion Pipelined: 18=(3t+6) POTRF+TRTRI+LAUUM: 25=(7t-3) Cholesky Factorization alone: 3t-2 Source: Julien Langou: ICL presentation 2011/02/04

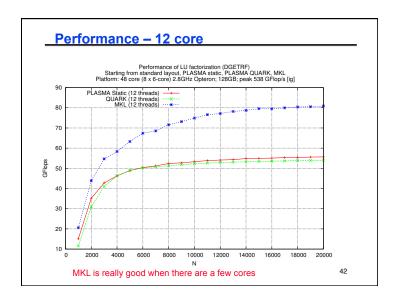
Simplified QUARK architecture Master Thread Worker Threads User Code Inserting tasks; Determining dependencies; Finding tasks; Queuing tasks Executing task; Checking descendants Insert Task T1 T1:Done Worker Queue: T3 Insert Task T2 T2:Done T4:Done Insert Task T3 Worker Queue: T5 Insert Task T4 T3:Queueo T5:Queued T7:Done Worker Queue: Insert Task T5 T6:NotReady T8:NotReady Insert Task T6 Insert Task T7 Insert Task T8 Scheduling is done using a combination of task assignment to workers (via locality reuse, etc) and work stealing. 04/21/2015 CS267 Lecture 25 39

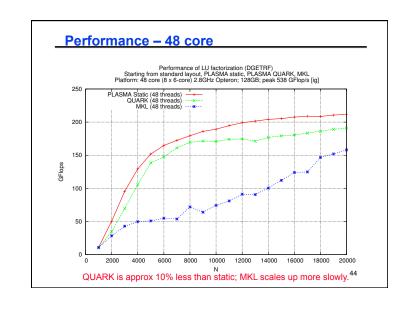
Scalability of DAG Schedulers

- How many tasks are there in DAG for dense linear algebra operation on an n x n matrix with b x b blocks?
- $O((n/b)^3) = 1M$, for n=10,000 and b = 100
- · Creating, scheduling entire DAG does not scale
- · PLASMA: static scheduling of entire DAG
- QUARK: dynamic scheduling of "frontier" of DAG at any one time

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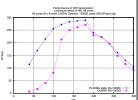




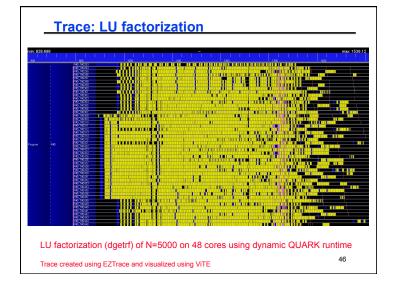


Limitations: Future Work

- VERY sensitive to task size
 - · For PLASMA, small tile sizes give bad performance, need NB around 180
 - Overhead kills performance for small tasks.



- · Master handles serial task insertion
 - · This is a hurdle for large scale scalability
 - Some work may be delegated in future versions
- Scalability
 - · Largest tests are for 48 cores
 - · Large scale scalability is untested
 - · For ongoing work see icl.cs.utk.edu/iclprojects/



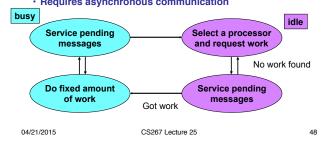
Distributed Task Queues

- The obvious extension of task queue to distributed memory is:
 - · a distributed task queue (or "bag")
 - · Idle processors can "pull" work, or busy processors "push" work
- When are these a good idea?
 - · Distributed memory multiprocessors
 - · Or, shared memory with significant synchronization overhead
 - · Locality is not (very) important
 - · Tasks may be:
 - · known in advance, e.g., a bag of independent ones
 - · dependencies exist, i.e., being computed on the fly
 - · The costs of tasks is not known in advance

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Distributed Dynamic Load Balancing

- Dynamic load balancing algorithms go by other names:
 - · Work stealing, work crews, ...
- Basic idea, when applied to tree search:
 - · Each processor performs search on disjoint part of tree
 - · When finished, get work from a processor that is still busy
 - · Requires asynchronous communication



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How to Select a Donor/Acceptor Processor

- Three basic techniques:
 - 1. Asynchronous round robin
 - Each processor k, keeps a variable "target,"
 - · When a processor runs out of work, requests work from target,
 - Set target_k = (target_k +1) mod procs
 - 2. Global round robin
 - · Proc 0 keeps a single variable "target"
 - · When a processor needs work, gets target, requests work from target
 - Proc 0 sets target = (target + 1) mod procs
 - 3. Random polling/stealing
 - When a processor needs work, select a random processor and request work from it
 - 4. Random distribution of work
 - When a processor has too much work, select a random processor to take it
- Repeat if no work is found

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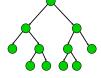
Theoretical Results (1)

Main result: Simple randomized algorithms are optimal with high probability

- · Others show this for independent, equal sized tasks
 - "Throw n balls into n random bins": ⊕ (log n / log log n) in fullest bin
 - · Throw d times and pick the emptiest bin: log log n / log d [Azar]
 - · Extension to parallel throwing [Adler et all 95]
 - · Shows p log p tasks leads to "good" balance



- Karp and Zhang show this for a tree of unit cost (equal size) tasks
 - · Parent must be done before children
 - · Tree unfolds at runtime
 - · Task number/priorities not known a priori
 - · Children "pushed" to random processors



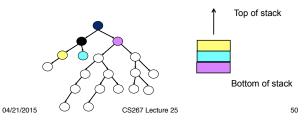
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How to Split Work

- First parameter is number of tasks to give when asked
 - Related to the self-scheduling variations, but total number of tasks is now unknown
- Second question is which one(s)
 - · Send tasks near the bottom of the stack (oldest)
 - · Execute from the top (most recent)
 - · May be able to do better with information about task costs



Theoretical Results (2)

Main result: Simple randomized algorithms are optimal with high probability

- Blumofe and Leiserson [94] show this for a fixed task tree of variable cost tasks
- their algorithm uses task pulling (stealing) instead of pushing, which is good for locality
 - · I.e., when a processor becomes idle, it steals from a random processor
 - · also have (loose) bounds on the total memory required
 - · Used in Cilk
 - · "better to receive than to give"
- Chakrabarti et al [94] show this for a dynamic tree of variable cost tasks
 - works for branch and bound, i.e. tree structure can depend on execution order
 - · uses randomized pushing of tasks instead of pulling, so worse locality

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Distributed Task Queue References

- Introduction to Parallel Computing by Kumar et al (text)
- · Multipol library (See C.-P. Wen, UCB PhD, 1996.)
 - · Part of Multipol (www.cs.berkeley.edu/projects/multipol)
 - Try to push tasks with high ratio of cost_to_compute/cost_to_push
 - Ex: for matmul, ratio = 2n³ cost(flop) / 2n² cost(send a word)
- Goldstein, Rogers, Grunwald, and others (independent work) have all shown
 - · advantages of integrating into the language framework
 - · very lightweight thread creation

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<u>Diffusion-Based Load Balancing</u>

- In the randomized schemes, the machine is treated as fully-connected.
- Diffusion-based load balancing takes topology into account
 - Send some extra work to a few nearby processors
 - · Average work with nearby neighbors
 - · Analogy to diffusion (Jacobi for solving Poisson equation)
 - Locality properties better than choosing random processor
 - · Load balancing somewhat slower than randomized
 - · Cost of tasks must be known at creation time
 - · No dependencies between tasks
- See Ghosh et al, SPAA96 for a second order diffusive load balancing algorithm
 - · takes into account amount of work sent last time
 - · avoids some oscillation of first order schemes

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Diffusion-based load balancing

- · The machine is modeled as a graph
- At each step, we compute the weight of task remaining on each processor
 - · This is simply the number if they are unit cost tasks
- Each processor compares its weight with its neighbors and performs some averaging
 - · Analysis using Markov chains
- See Ghosh et al, SPAA96 for a second order diffusive load balancing algorithm
 - · takes into account amount of work sent last time
 - · avoids some oscillation of first order schemes
- Note: locality is still not a major concern, although balancing with neighbors may be better than random

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Charm++

Load balancing based on Overdecomposition

- Context: "Iterative Applications"
 - · Repeatedly execute similar set of tasks
- Idea: decompose work/data into chunks (chares in Charm++), and migrate chares for balancing loads
 - Chares can be split or merged, but typically less frequently (or unnecessary in many cases)
- How to predict the computational load and communication between objects?
 - · Could rely on user-provided info, or based on simple metrics
 - (e.g. number of elements)
 - · Alternative: principle of persistence
 - · Statistics change slowly, can rebalance occasionally
- · Software, documentation at charm.cs.uiuc.edu
 - \bullet Many applications: NAMD, LeanMD, OpenAtom, ChaNGa, ... $_{\rm 56}$

Source: Laxmikant Kale

Measurement Based Load Balancing in Charm++

- Principle of persistence (A Heuristic)
 - Object communication patterns and computational loads tend to persist over time, so recent past good predictor of future
 - In spite of dynamic behavior
 - · Abrupt but infrequent changes
 - · Slow and small changes
 - · Only a heuristic, but applies on many applications
- · Measurement based load balancing
 - Runtime system (in Charm++) schedules objects and mediates communication between them, so can measure load
 - Use the instrumented data-base periodically to make new decisions, and migrate objects accordingly
- Charm++ provides a suite of strategies, and plug-in capability for user-defined ones
 - Also, a meta-balancer for deciding how often to balance, and what type of strategy to use
 Source: Laxmikant Kale 57

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Periodic Load Balancing Strategies

- · Many alternative strategies can use the same database
 - · OCG: Object communication graph
 - Or simply #loads of each object, if communication unimportant
- Centralized strategies: collect data on one processor
 - Feasible on up to a few thousand cores, because number of objects is typically small (10-100 per core?)
 - Use Graph partitioners, or greedy strategies
 - Or refinement strategies: mandated to keep most objects on the same processors
 - Charm++ provides a suite of strategies, and plug-in capability for user-defined ones
 - Also, a meta-balancer for deciding how often to balance, and what type of strategy to use

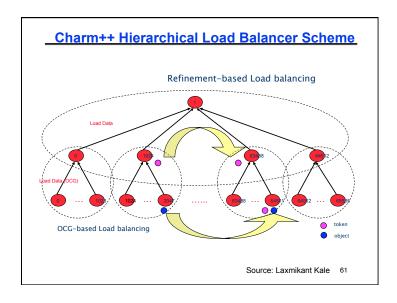
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Regular Timesteps Detailed, aggressive Load Balancing Timesteps Refinement Load Balancing O4/21/2015 CS267 Lecture 25 Source: Laxmikant Kale 59

Periodic Load Balancing for Large machines

- Two Challenges:
- Object communication graph cannot be brought to one processor
 - A solution : Hierarchical load balancer (next slide)
- · Interconnection topology must be taken into account
 - Limited bisection bandwidth (on Torus networks, for example)
 - Solution: topology-aware balancers (later slides)

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Topology-aware load balancing

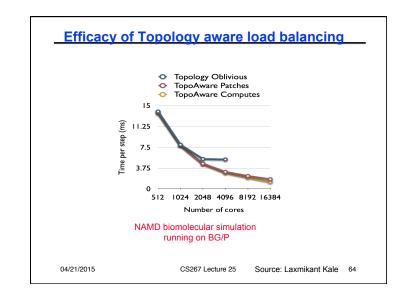
- With wormhole routing, the number of hops a message takes has very little impact on transit time
 - · But: On an unloaded network!
- · But bandwidth is a problem
 - · Especially on torus networks
 - More hops each message takes, more bandwidth they occupy
 - · Leading to contention and consequent delays
- · So, we should place communicating objects nearby
 - Many current systems are "in denial" (no topo-aware allocation)
 - · Partly because some applications do well
 - · Lot of research in the 1980's
 - But not very relevant because of technological assumptions and topologies considered
 - Ex: Take advantage of physical proximity (domain decomp.)

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Topology aware load balancing (2/2)

- Metric: Average dilation (equivalently, sum of hop-bytes)
- Object-based over-decomposition helps balancing
- · When (almost) near-neighbor communication dominates
 - · And geometric information available
 - · Simplest case, but challenges: Aspect ratios, load variations,
 - · Strategies: ORB, many heuristic placement strategies
 - · (A. Bhatele Phd. Thesis)
 - Variation: A set of pairwise interactions (e.g. Molecular dynamics) among geometrically placed primary objects:
 - Strategy: place within the "brick" formed by the two primary objs
- When application has multiple phases:
 - Strategy: often blocking helps. Alternatively, optimize one phase (better than optimizing neither)
 - Example: OpenAtom for Quantum Chemistry

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Summary and Take-Home Messages

- There is a fundamental trade-off between locality and load balance
- · Many algorithms, papers, & software for load balancing
- Key to understanding how and what to use means understanding your application domain and their target
 - Shared vs. distributed memory machines
 - Dependencies among tasks, tasks cost, communication
 - Locality oblivious vs locality "encouraged" vs locality optimized
 Computational intensity: ratio of computation to data movement cost
 - When you know information is key (static, semi, dynamic)
- Open question: will future architectures lead to so much load imbalance that even "regular" problems need dynamic balancing?

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