

$$\sum_i S_i b_i = \left( \sum_i P_i a_i \right) / \left( \sum_j h_j a_j \right)$$